

WINTON INAUGURAL SYMPOSIUM

# ENERGY EFFICIENCY...

...fundamental physical limits



Cambridge,  
1<sup>st</sup> October 2012

## Limits to efficiency of photovoltaic energy conversion

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**Imperial College**  
London



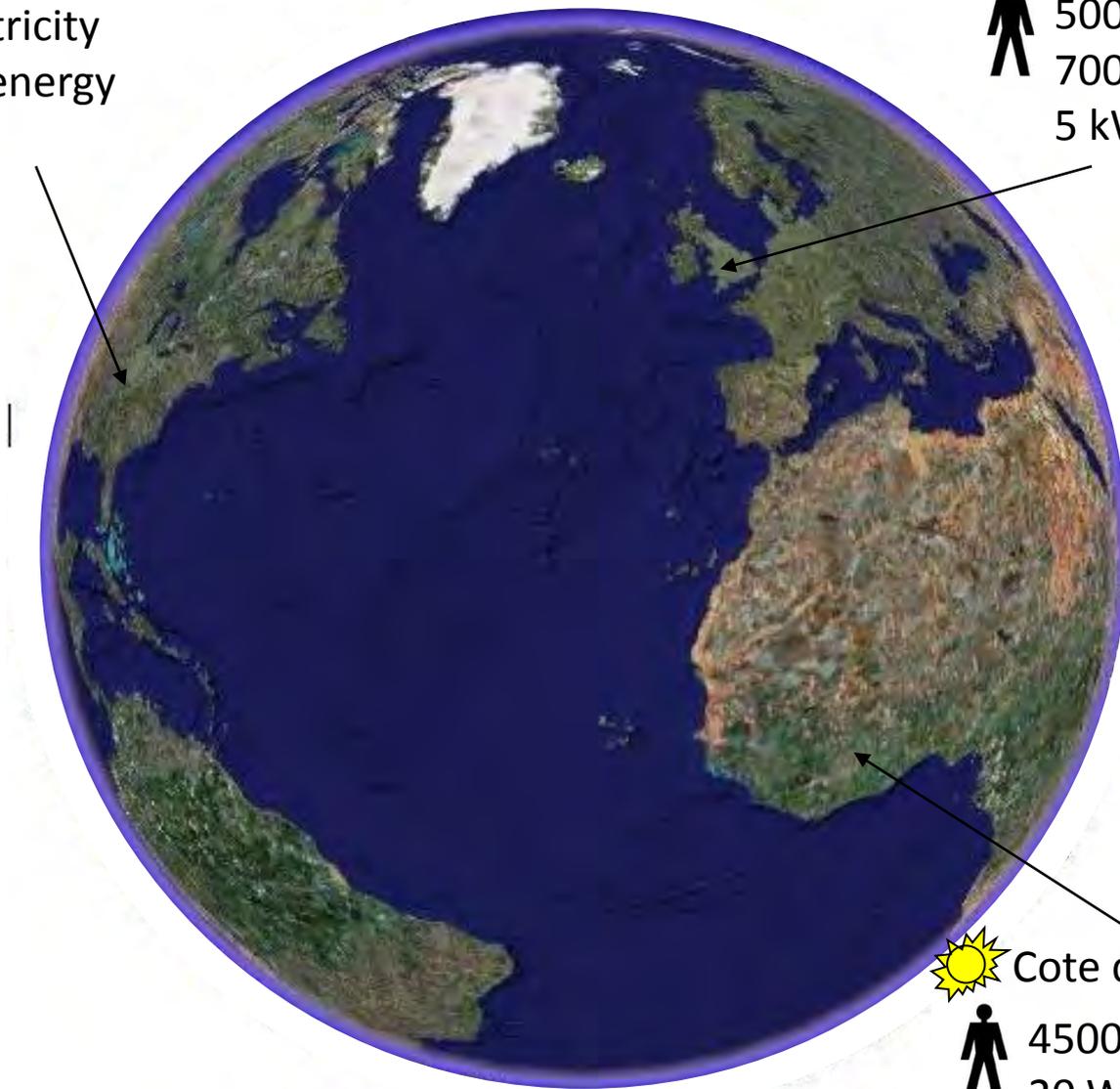
# Energy from the Sun

 USA:  $\sim 200 \text{ Wm}^{-2}$

 6500 kW solar resource  
1500 W electricity  
10 kW total energy

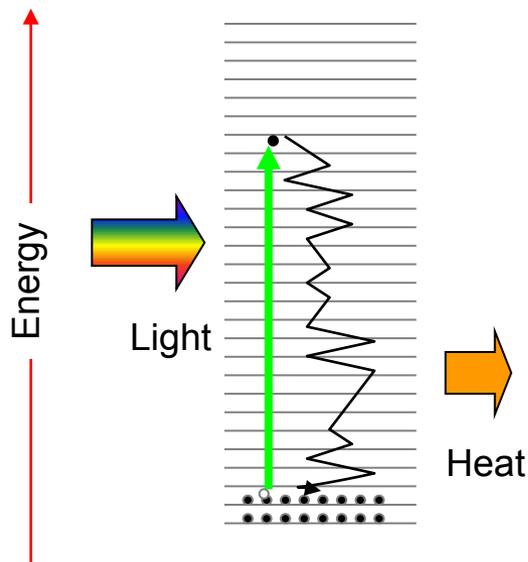
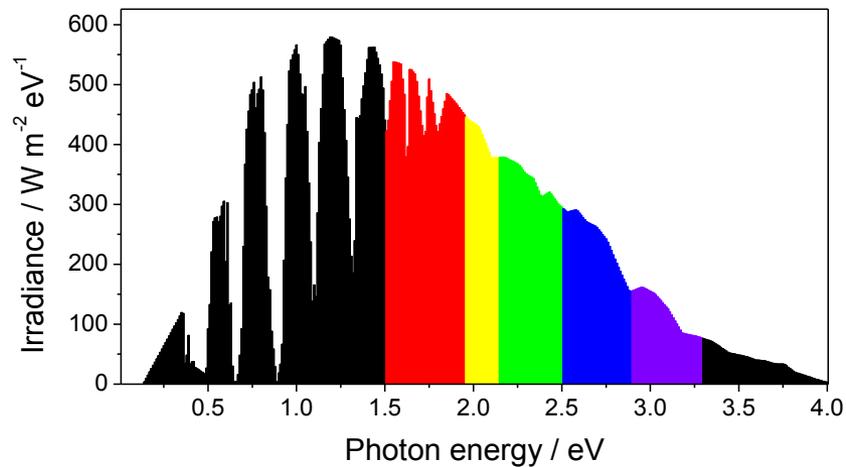
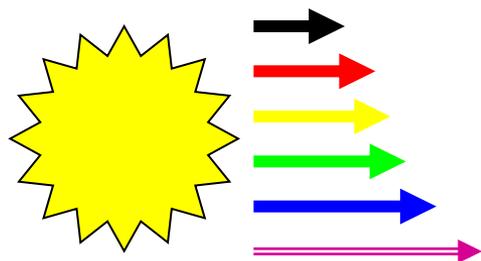
 UK:  $125 \text{ Wm}^{-2}$

 500 kW solar resource  
700 W electricity  
5 kW total energy

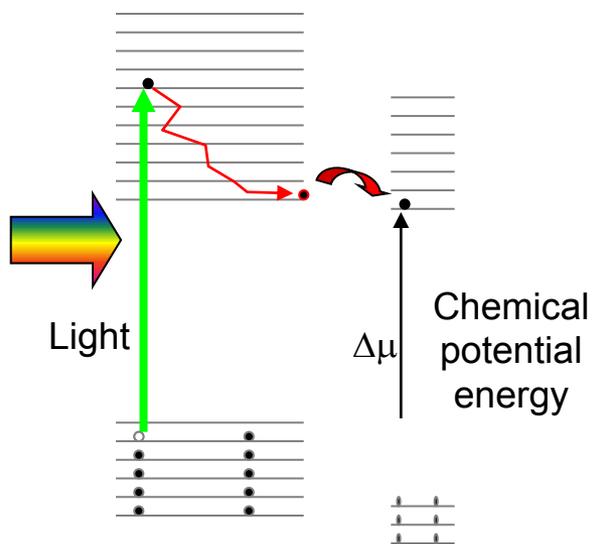


 Cote d'Ivoire:  $\sim 250 \text{ Wm}^{-2}$

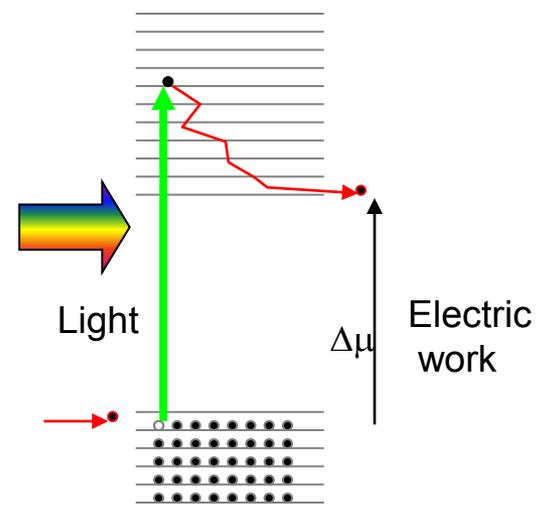
 4500 kW solar resource  
20 W electricity  
0.5 kW total energy



Solar thermal

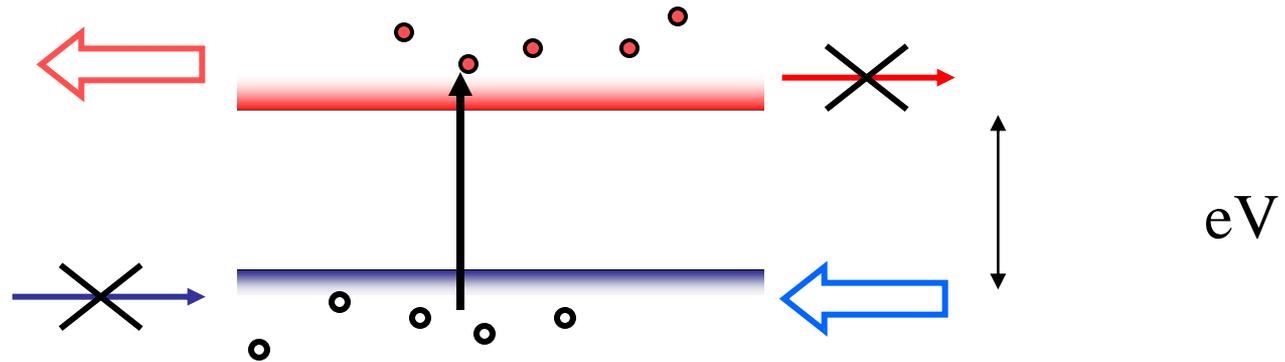


Solar chemical



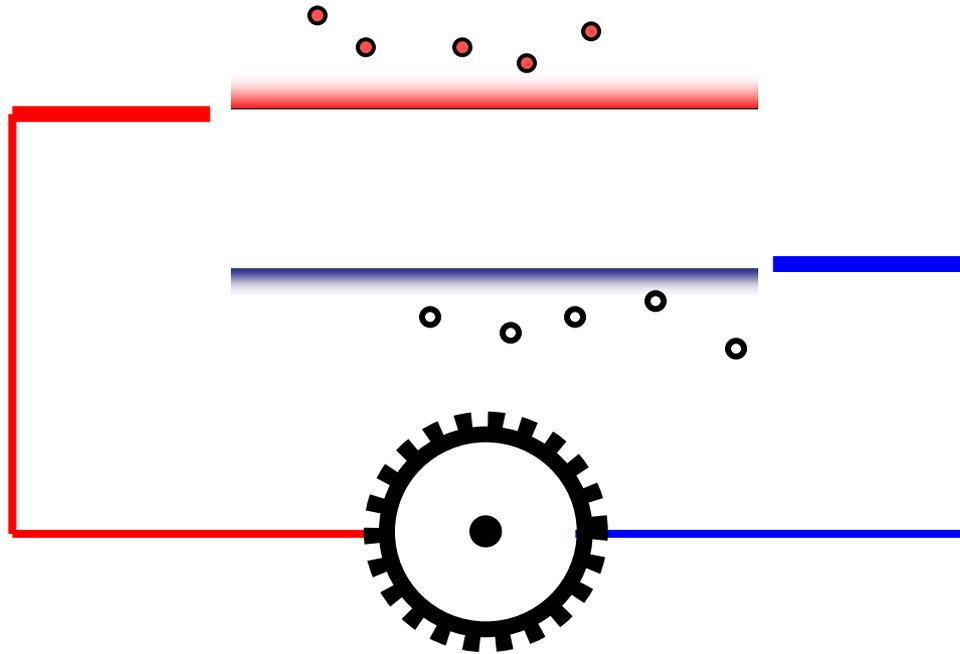
Solar photovoltaic

# Photons in, electrons out

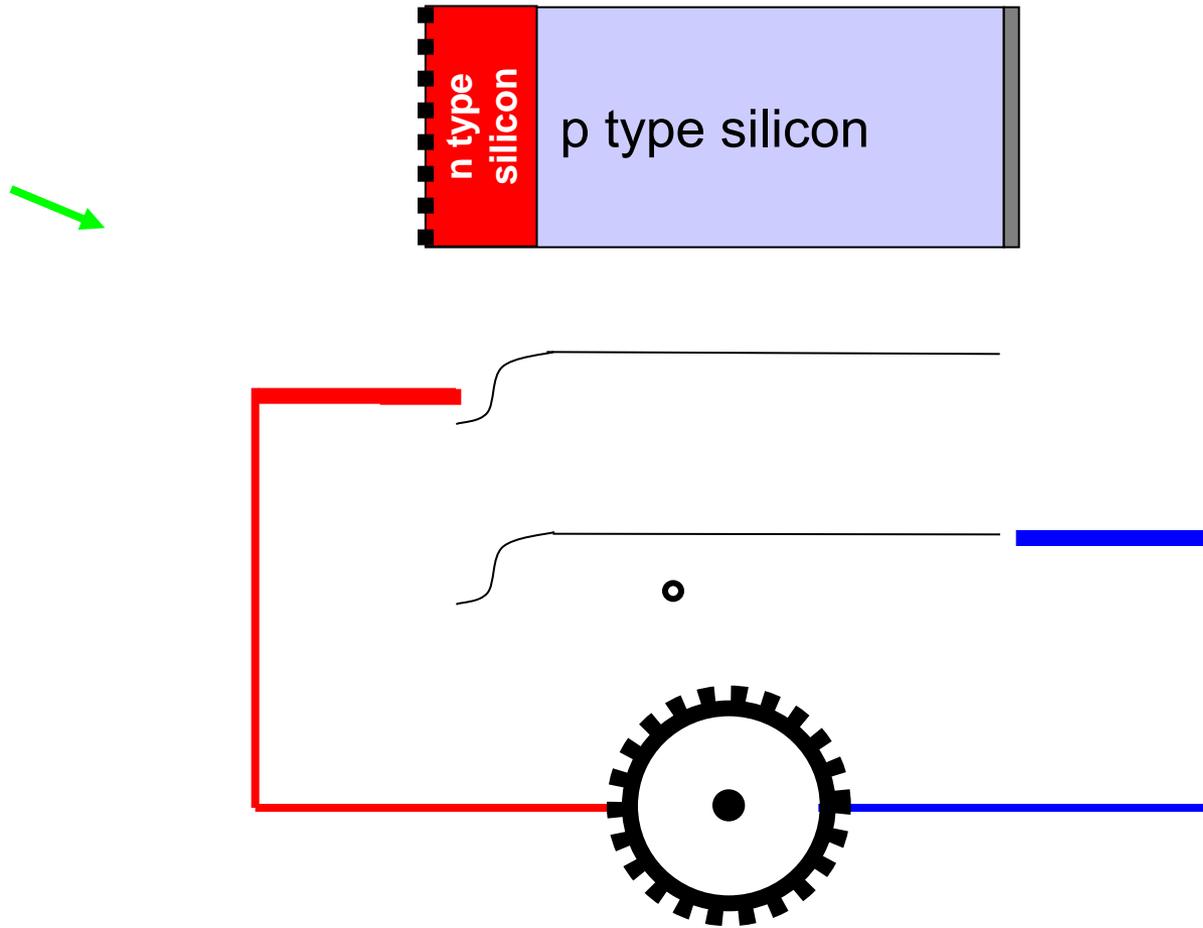


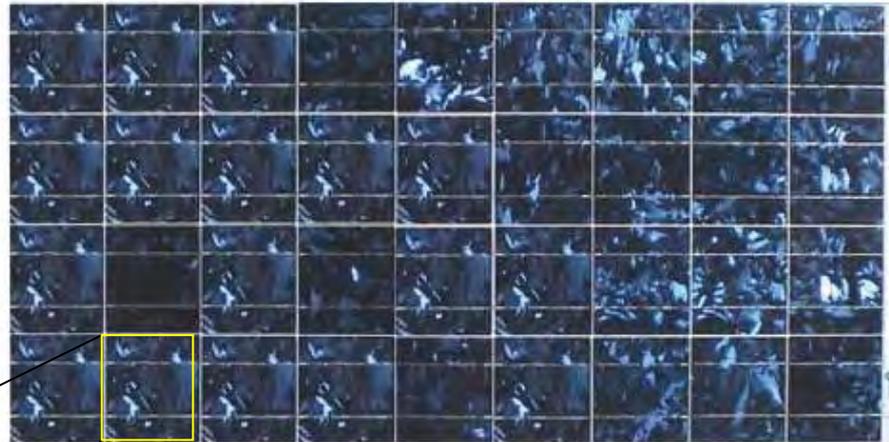
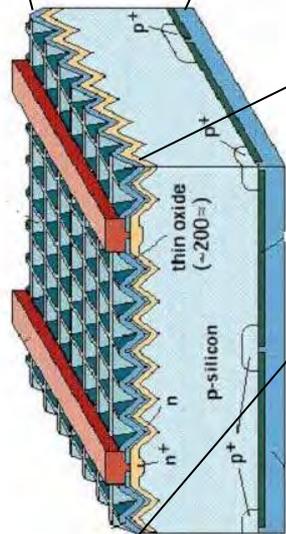
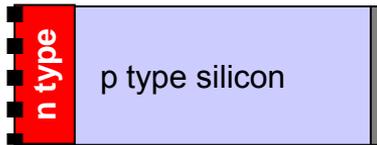
- Photovoltaic energy conversion requires:
  - photon **absorption** across an energy gap
  - **separation** of photogenerated charges
  - **asymmetric contacts** to an external circuit

# Photons in, electrons out



# Photons in, electrons out





efficiency  
~ 15-20%

power rating  
~ 100-200 W<sub>p</sub>



Applications, large and small



Solar powered refrigeration  
~100 W<sub>p</sub>

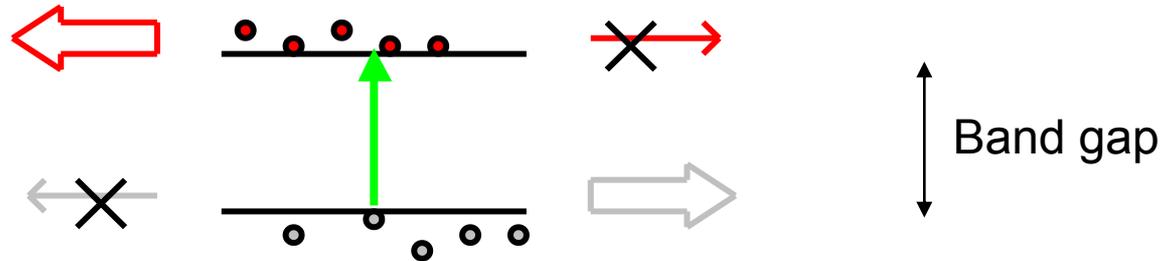


~1 mW<sub>p</sub>

# Outline

- Photovoltaic energy conversion
- **Limiting efficiency of solar cells**
- Where next?
- Routes to more work per photon
- Molecular solar cells

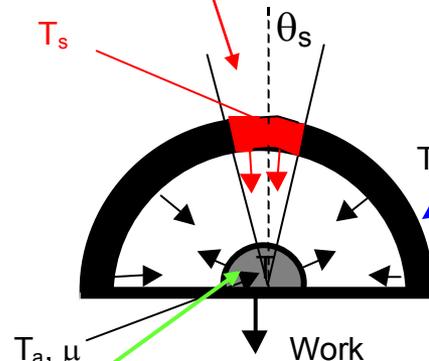
# Detailed balance limit



- (i) One electron hole pair per photon with  $h\nu > E_g$ ,
- (ii) Carriers relax to form separate Fermi distributions at lattice temperature  $T_{\text{ambient}}$  with quasi Fermi levels separated by  $\Delta\mu$ .
- (iii) All electrons extracted with same electrochemical potential  $\Delta\mu = eV$
- (iv) Only loss process is spontaneous emission

# Detailed balance limit

A fraction  $X\beta$  of the “sky” emits solar radiation at a black body temperature of  $T_{\text{sun}}$

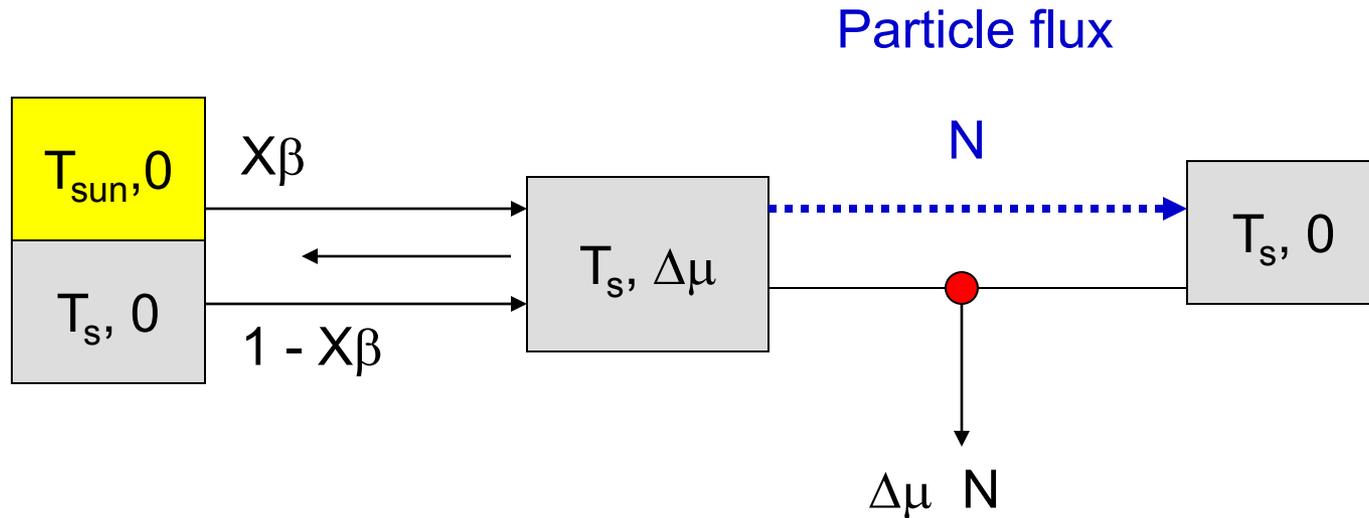


A fraction  $(1 - X\beta)$  of the “sky” emits ambient radiation at a black body temperature of  $T_{\text{ambient}}$

The photovoltaic energy converter emits ambient radiation at a black body temperature of  $T_{\text{ambient}}$  and a chemical potential of  $\Delta\mu$

The remaining charge pairs provide a current of electrons with chemical potential of  $\Delta\mu$

# Calculation of limiting efficiency

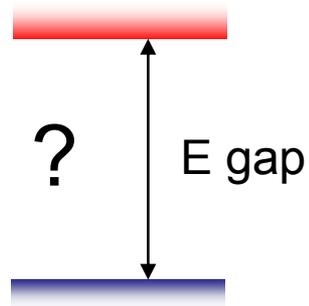
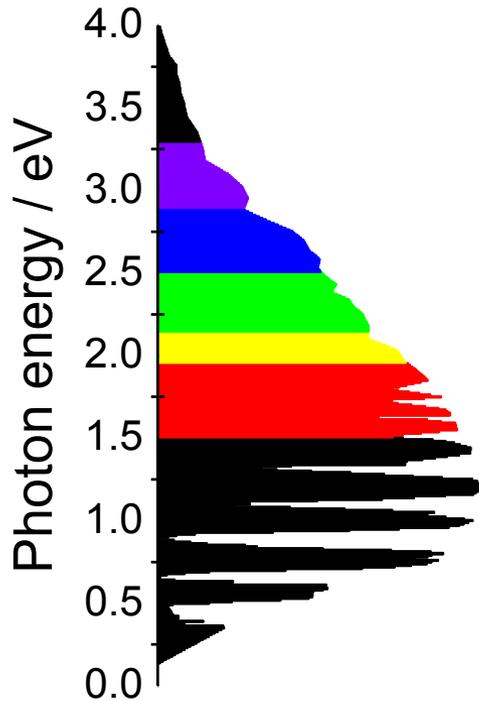


$$\frac{J}{e} = X\beta \int_{E_g}^{\infty} b_{sun}(E) dE + (1 - X\beta) \int_{E_g}^{\infty} b_{ambient}(E) dE - e^{\Delta\mu/kT} \int_{E_g}^{\infty} b_{ambient}(E) dE$$

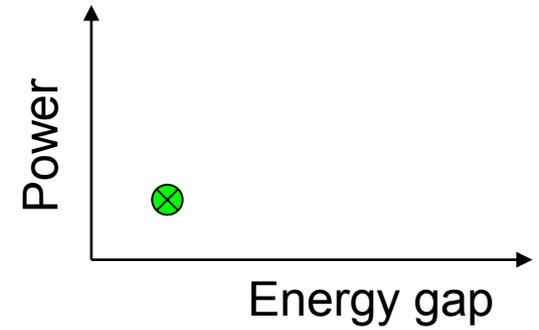
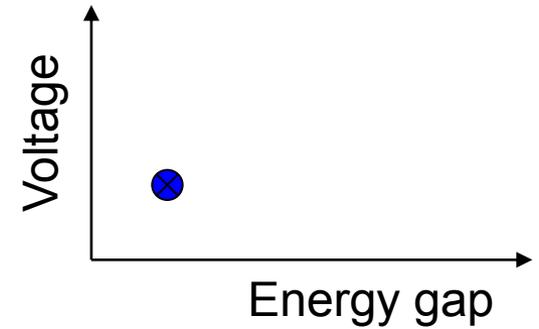
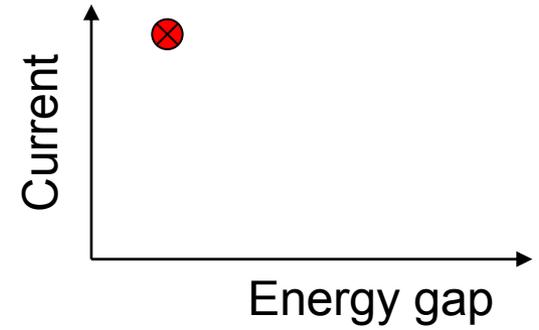
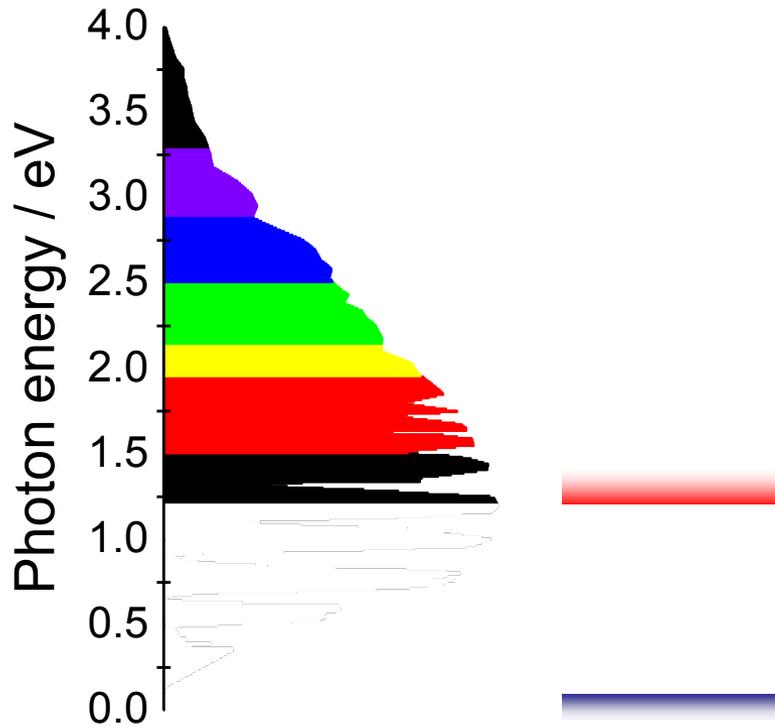
$$J = J_{sc} - J_0 \left( e^{eV/kT} - 1 \right)$$

$$P = JV$$

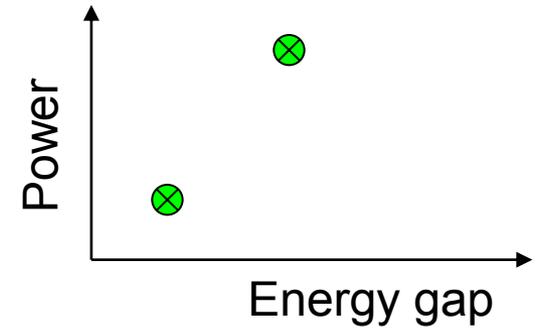
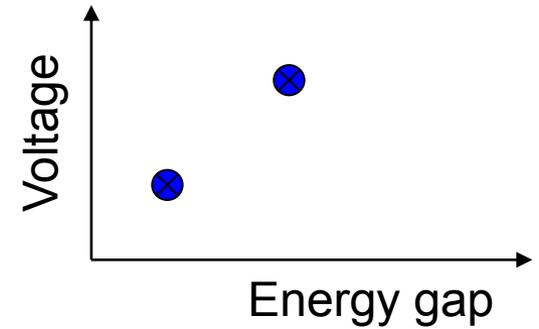
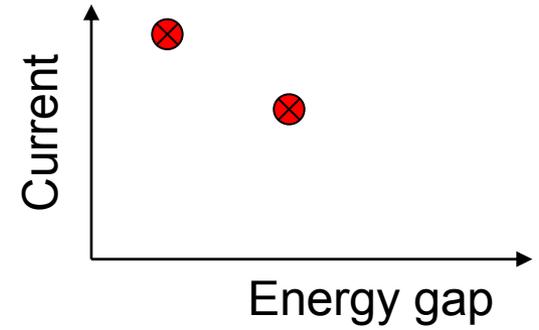
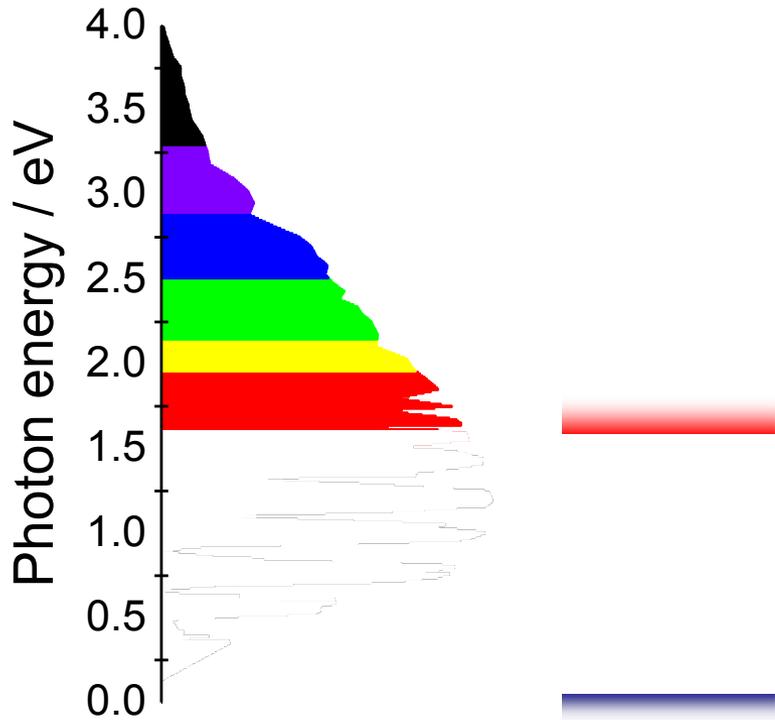
# Limit to efficiency: the Goldilocks story



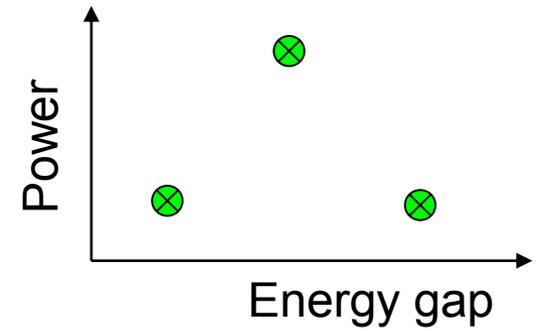
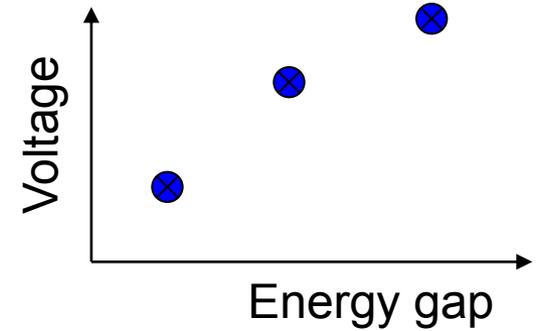
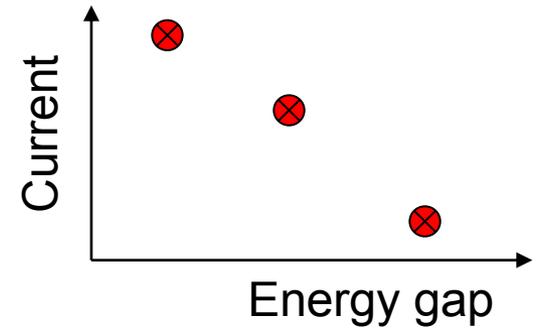
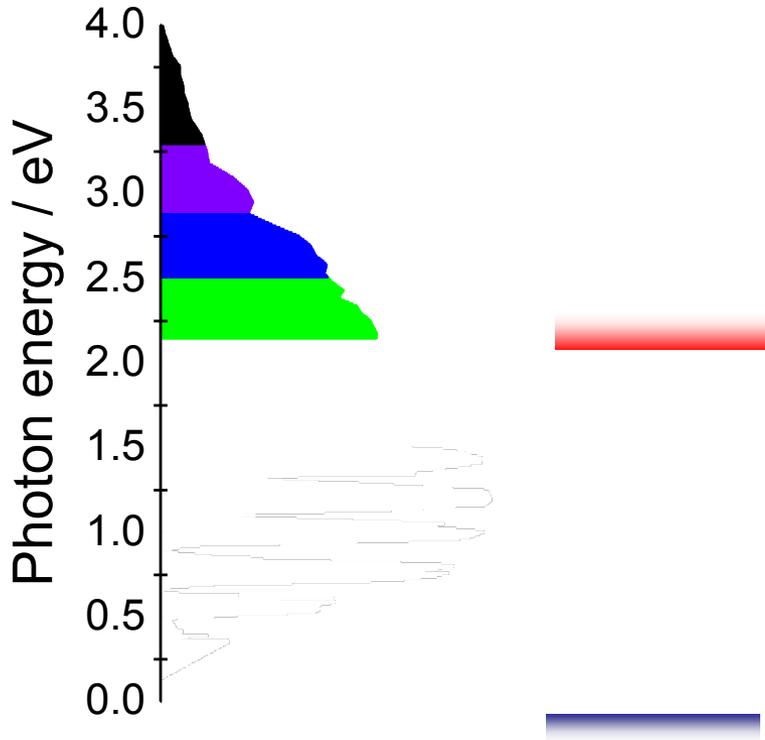
# Limit to efficiency: the Goldilocks story



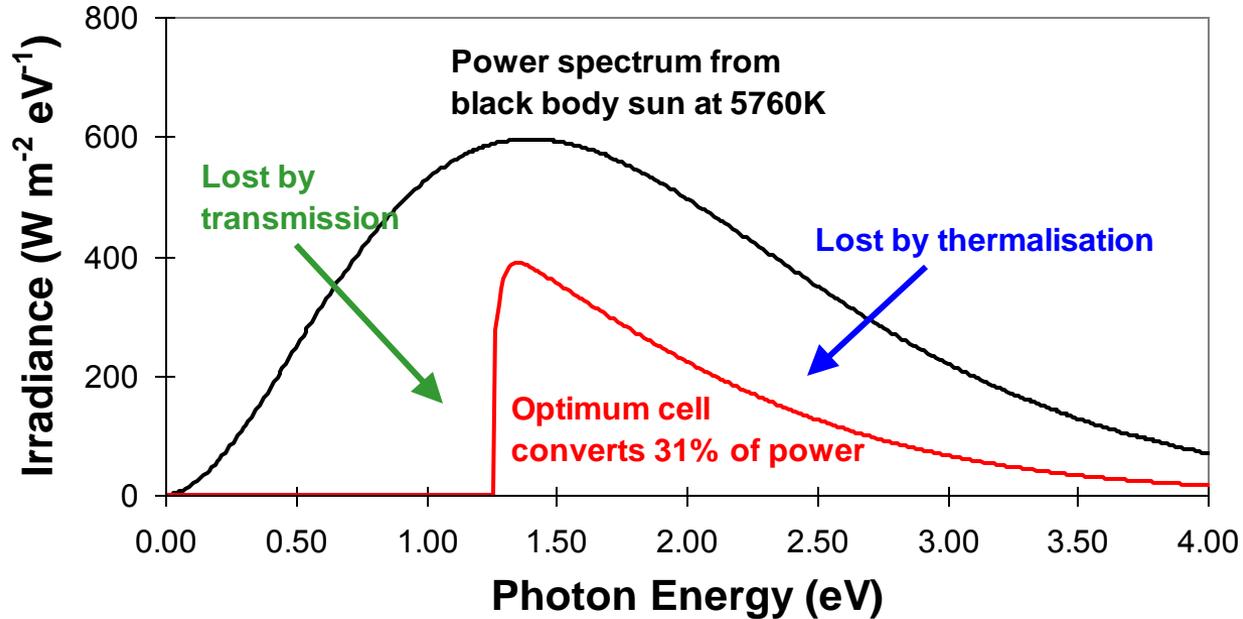
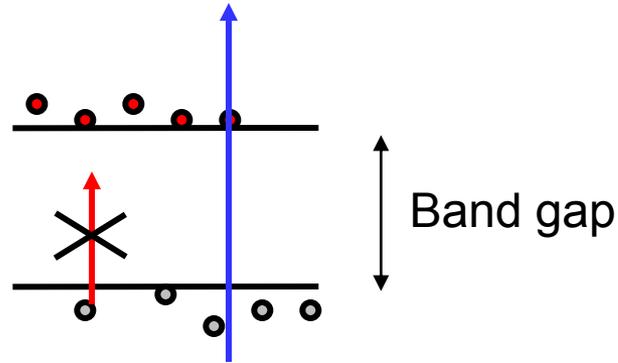
# Limit to efficiency: the Goldilocks story



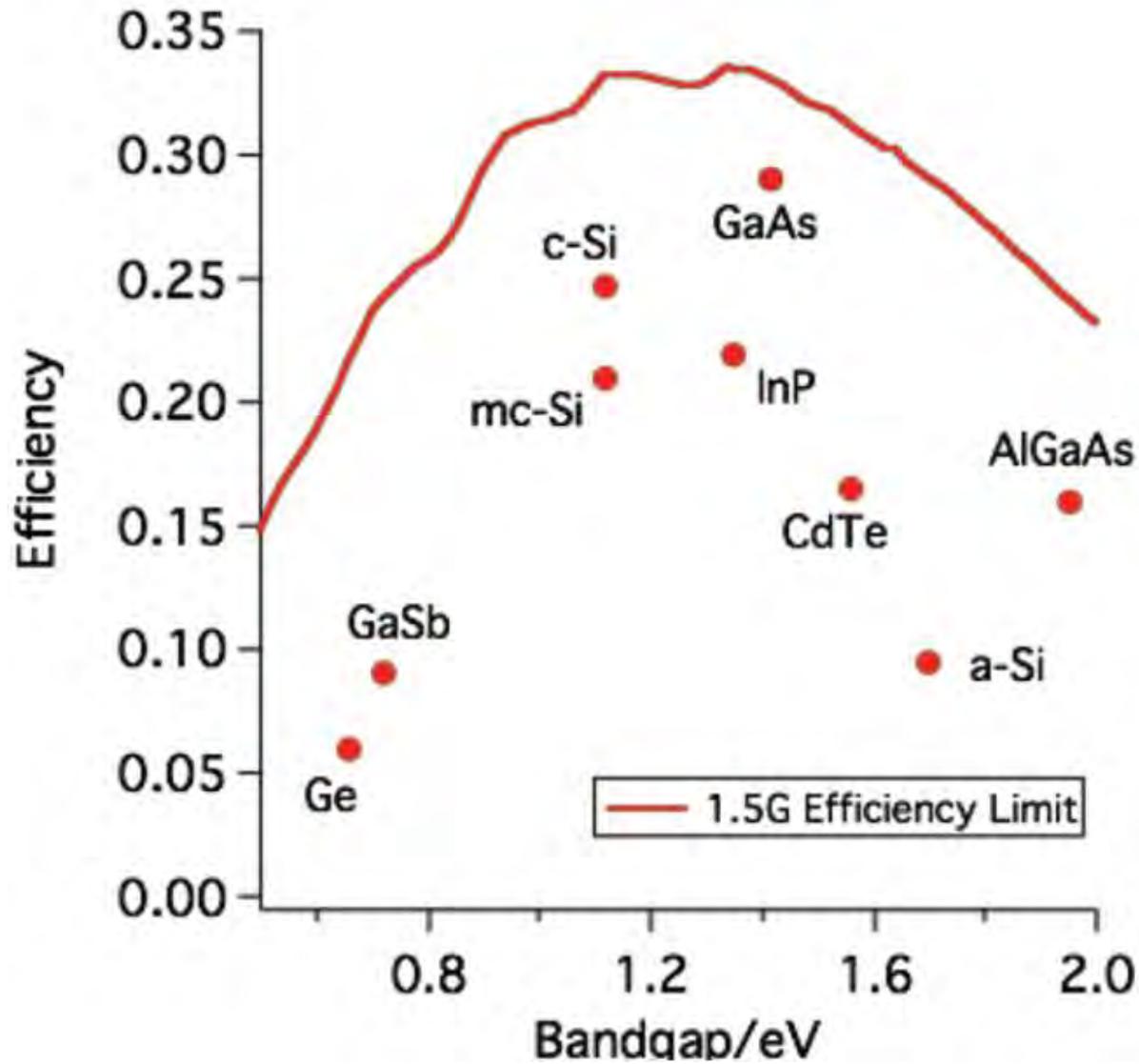
# Limit to efficiency: the Goldilocks story



# Limiting efficiency of single band gap cell



# Practical and limiting efficiencies



# How bad are the assumptions?

(i) One electron hole pair per photon with  $h\nu > E_g$ ,

Overestimate current by 10-20%

(ii) Carriers relax to form separate Fermi distributions at lattice temperature  $T_{\text{ambient}}$  with quasi Fermi levels separated by  $\Delta\mu$ .

~ OK

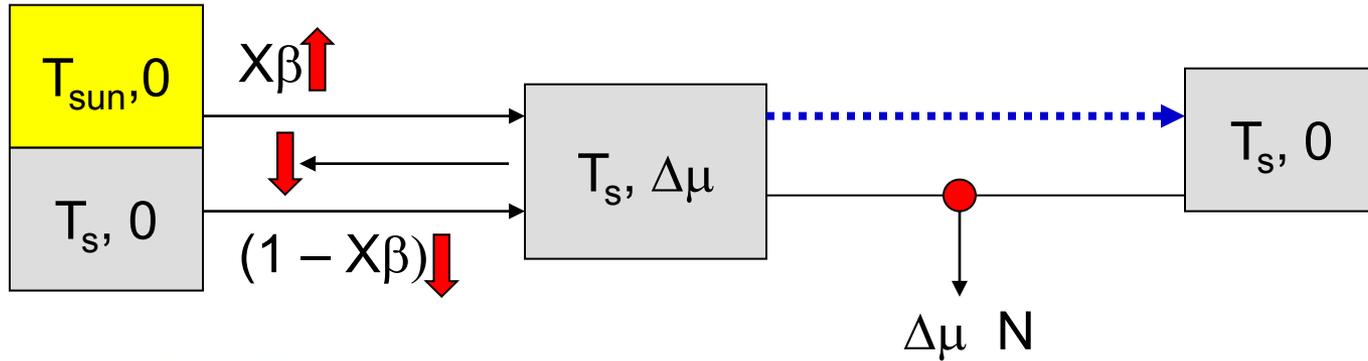
(iii) All electrons extracted with same electrochemical potential  $\Delta\mu = eV$

Overestimate  $eV_{\text{oc}}$  by  $O(0.1 \text{ eV})$

(iv) Only loss process is spontaneous emission

Overestimate  $eV_{\text{oc}}$  by few 0.1 eV  
Overestimate fill factor

# Highest efficiency single junction: thin film GaAs



Device with absorbing substrate



Limiting efficiency: 30.4 %  
Actual efficiency: 24.8 %

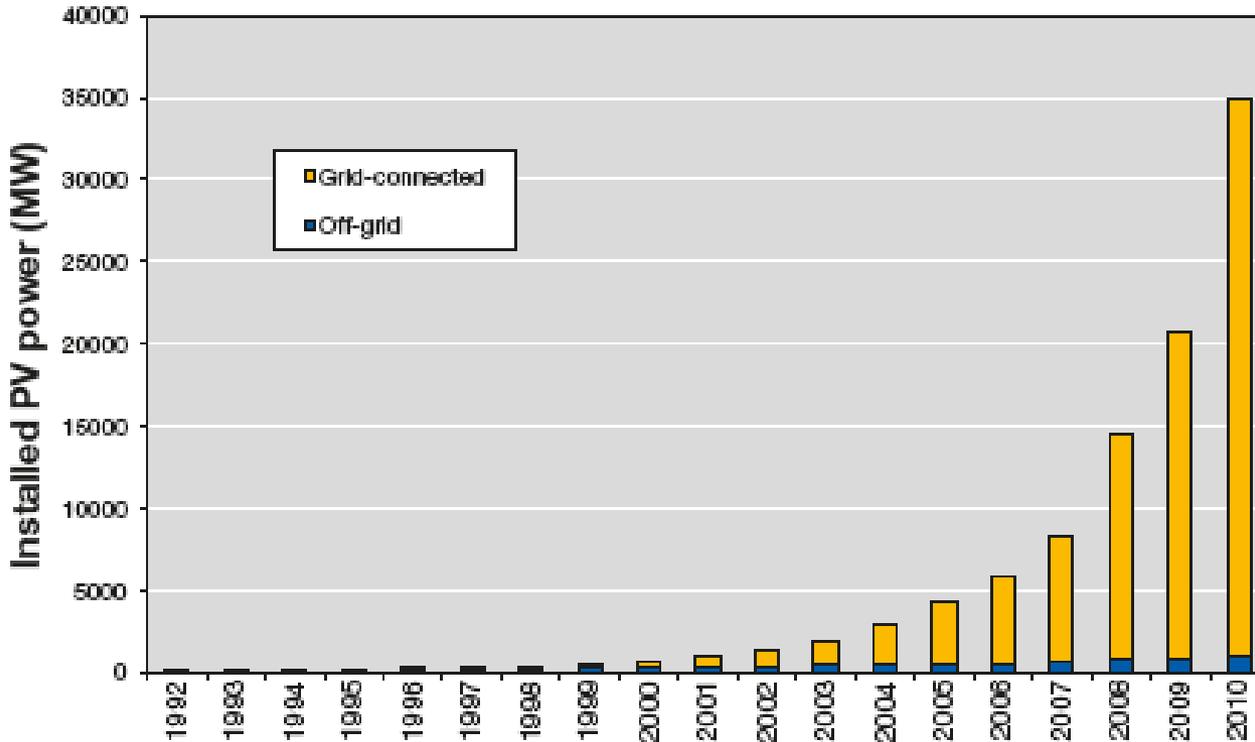
Thin-film device



Limiting efficiency: 32.4 %  
Actual efficiency: 28.8 %

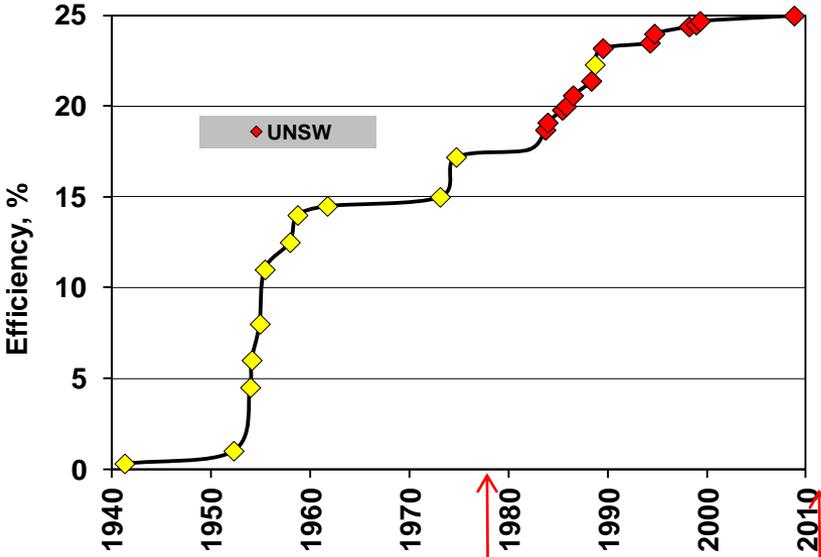
# Outline

- Photovoltaic energy conversion
- Limiting efficiency of solar cells
- **Where next?**
- Routes to more work per photon
- Molecular solar cells



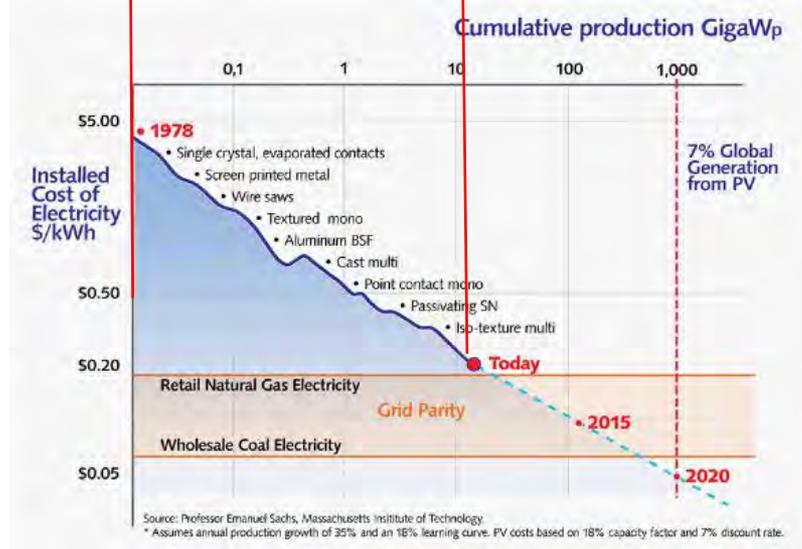
- Installed PV capacity growing at > 30% per annum for ~15 years
- Mainly based on crystalline Si technology
- Where next?

Courtesy: Martin Green



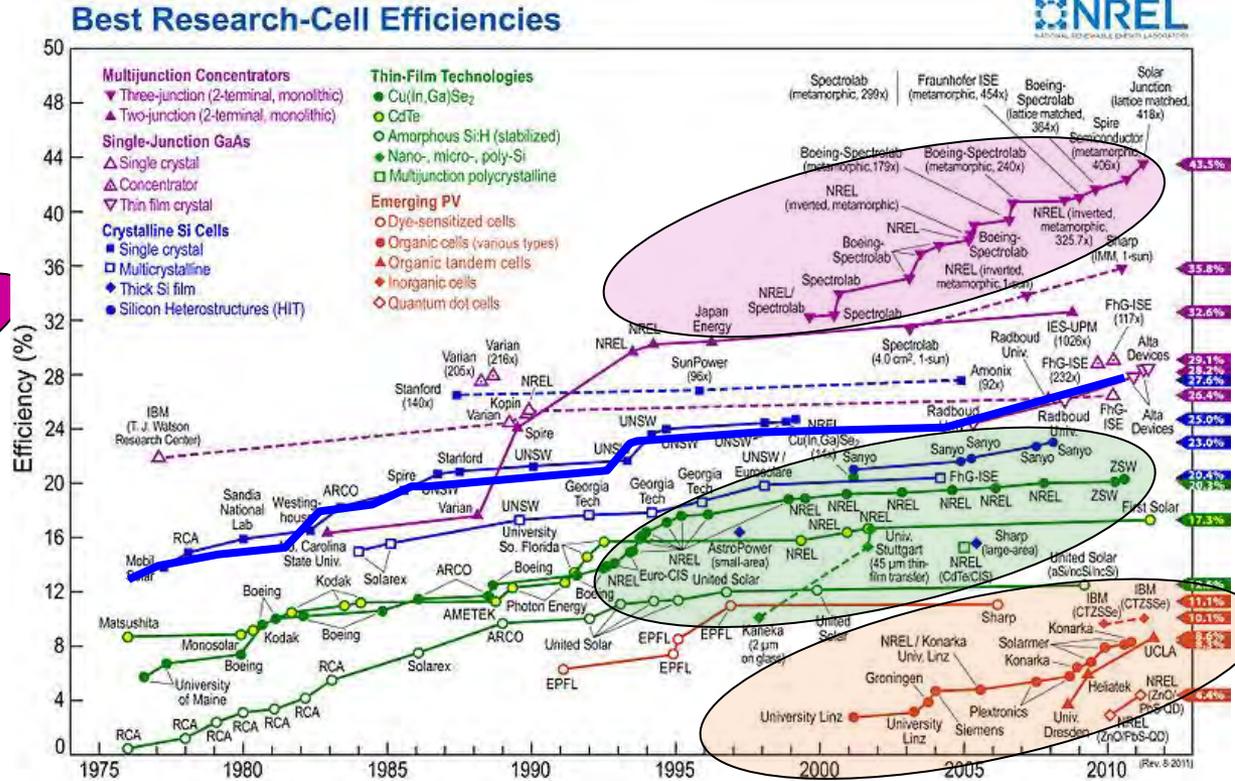
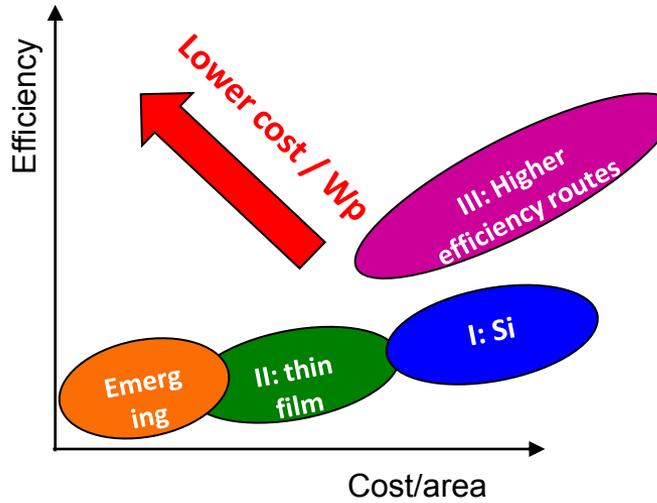
Cost reductions follow maturing of Si technology through innovations in manufacturing and design.

Cost evolution typical of a semiconductor technology not a conventional energy technology



Role for technical innovation?

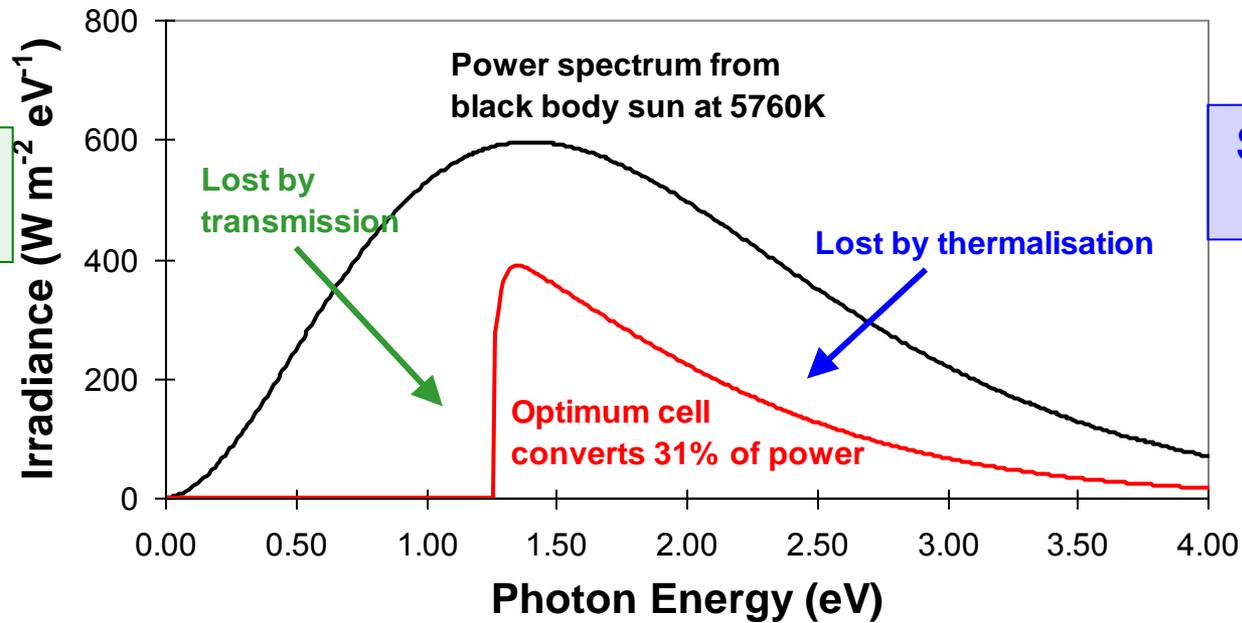
# PV technologies



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# Routes to more work per photon

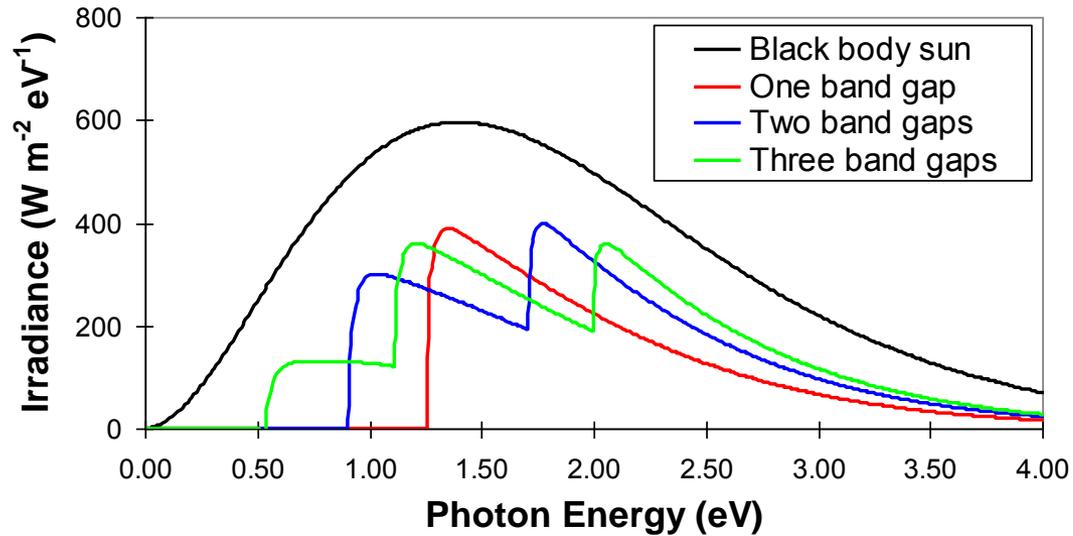
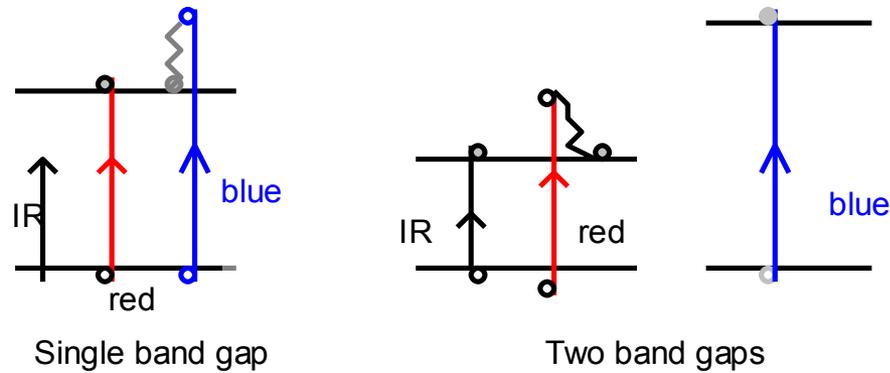


Spectral conversion

Slow carrier cooling

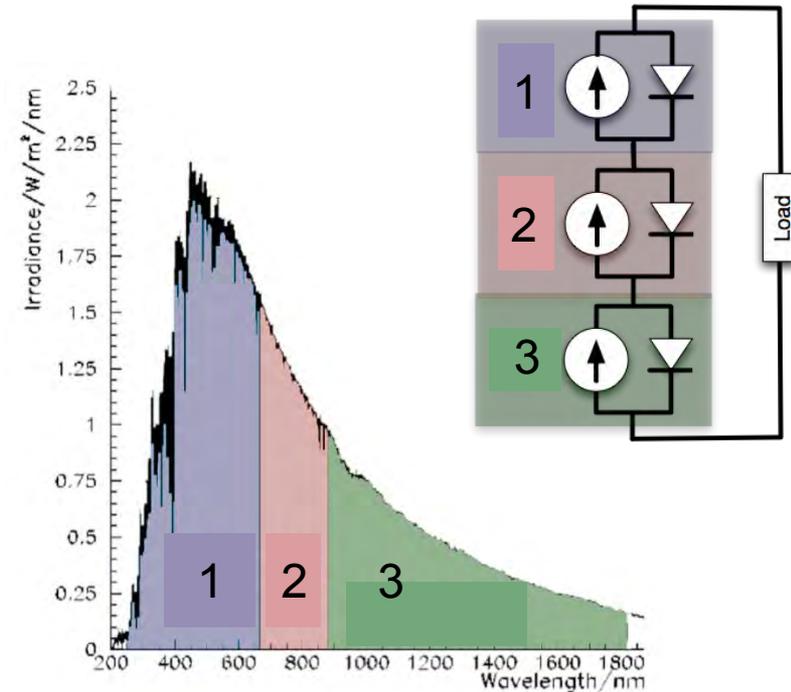
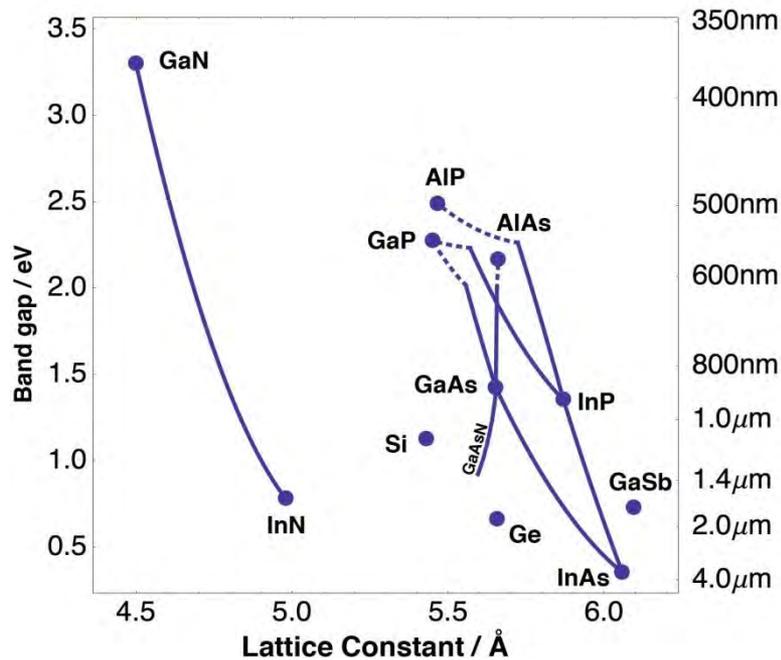
More band gaps

# Route 1: Multiple band gaps



- Multi-junction structures or spectral splitting

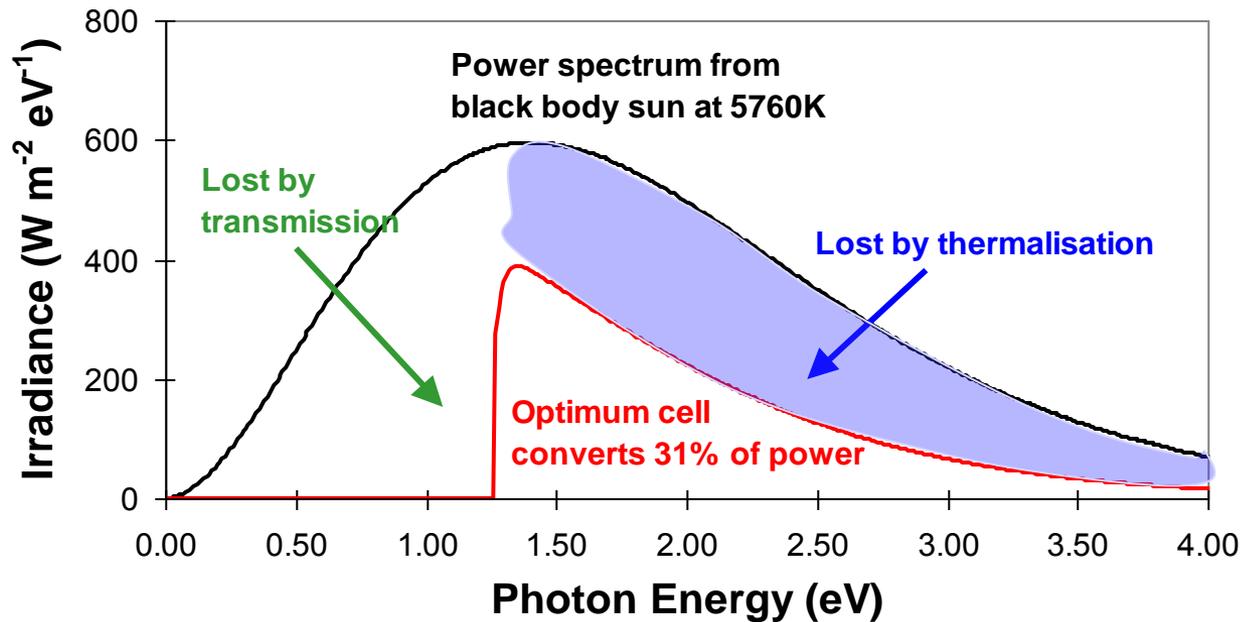
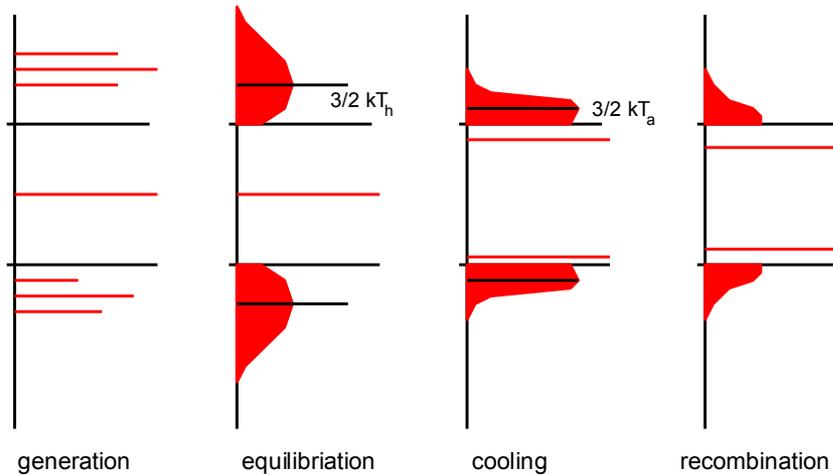
# III-V Multi-Junction Solar Cells



- Wide range of band gaps available but seek combinations with similar lattice constant
- Record of 43.5% by Solar Junction (April 2011) for a triple junction using dilute nitride (InGaP/GaAs/InGaAsN)

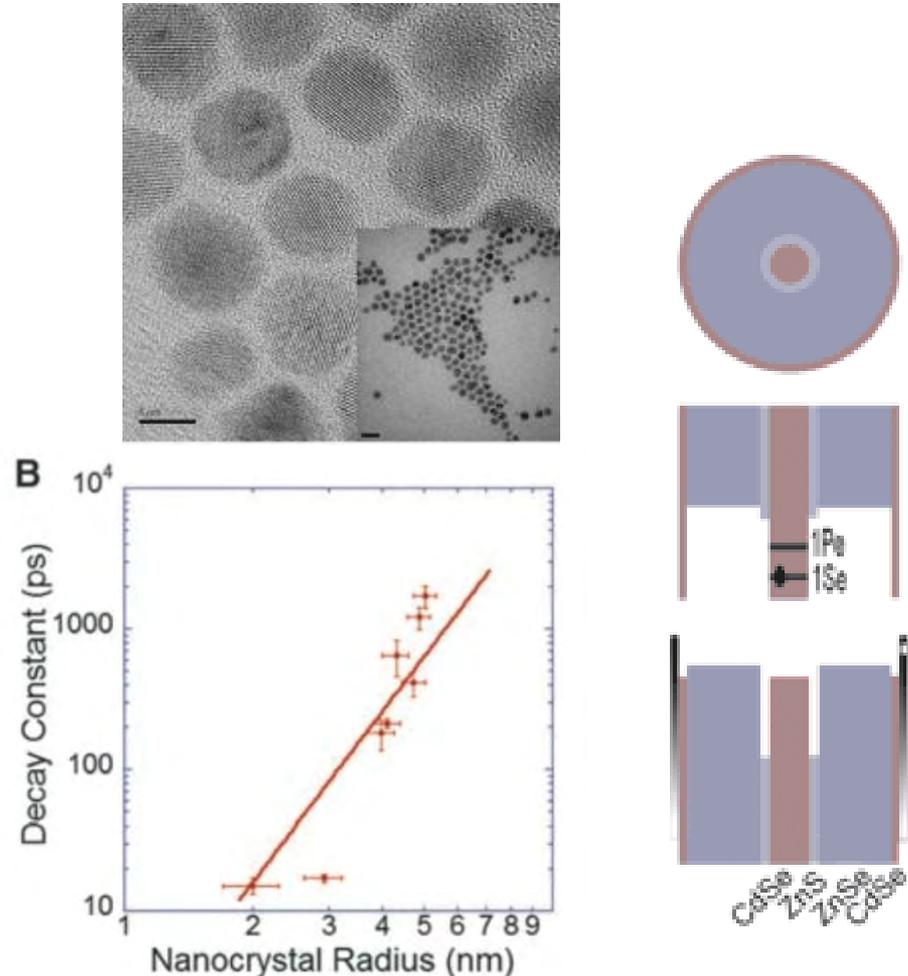
**This works, but multijunction III-V structures are expensive to grow**

# Route 2: More work per photon by slowed cooling



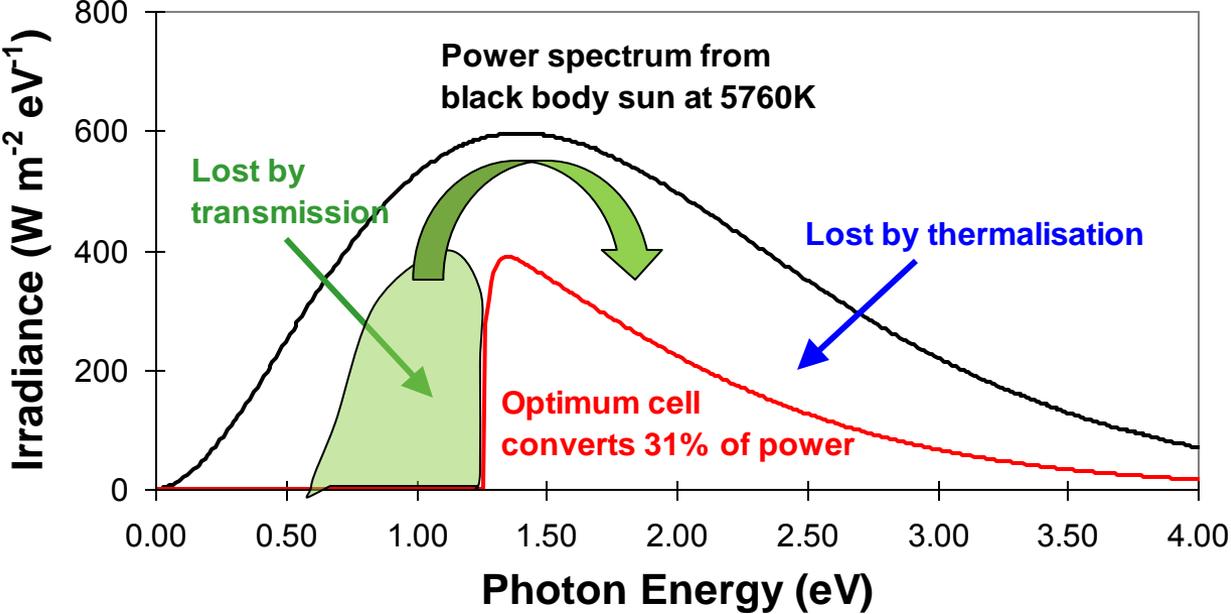
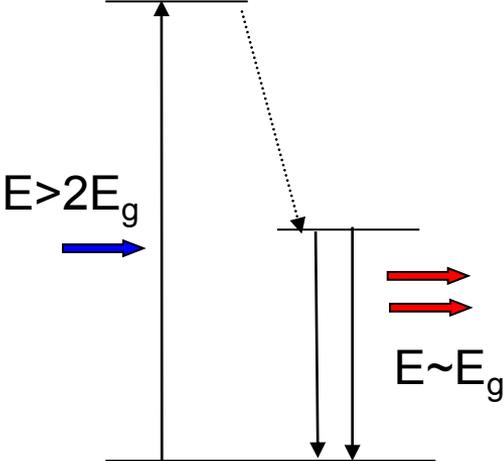
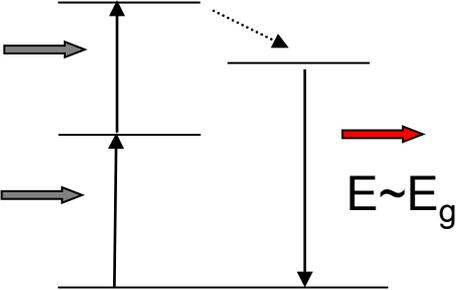
# Strategies for slowing carrier cooling

- Exploit limited electronic and photon states in nano- or molecular systems
- Carrier cooling slowed down in quantum dots by 'phonon bottleneck' effect
- Enhance this with strategies to prevent recombination
  - Core-shell structure, interface passivation, ligands
  - Cooling slowed by 3 orders

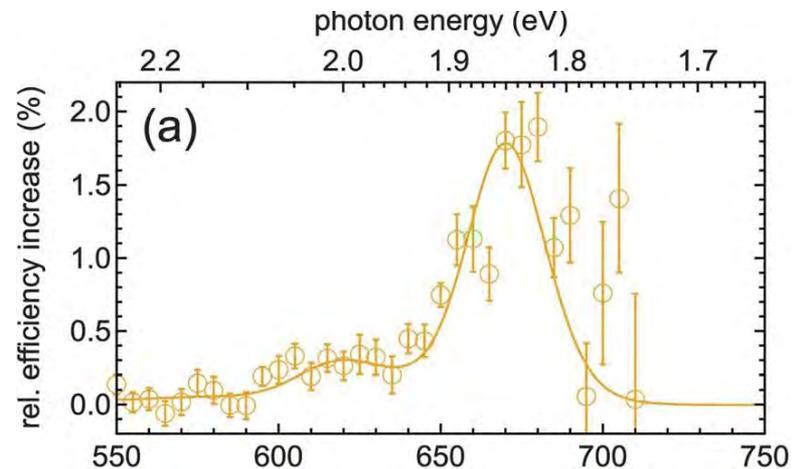
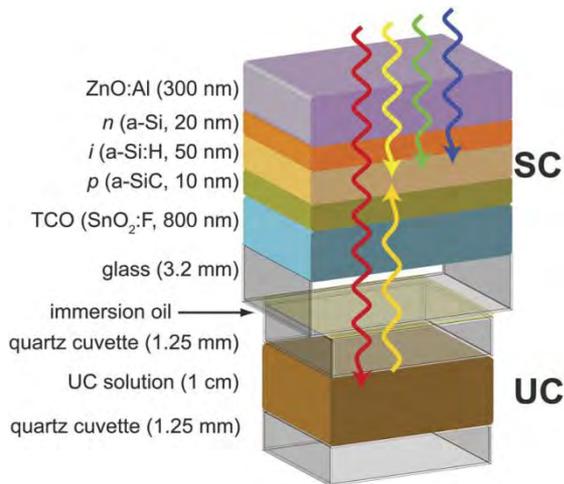
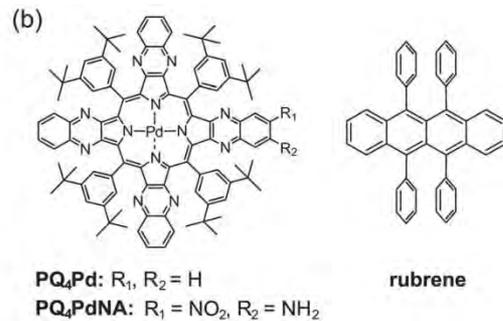
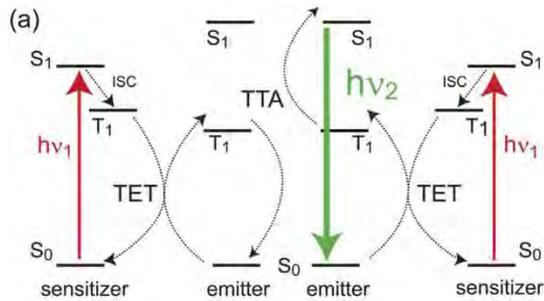


**Evidence for slowed cooling but tiny effect at solar intensities**

# Route 3: Reshaping the spectrum by up and down-conversion



# Molecular up-conversion: applied to a-Si solar cell



- Absorption in red absorbing molecules → triplet formation → triplet transfer to emitter → singlet regeneration → emission
- Applied to a-Si:H solar cell to increase EQE

**Evidence for both up- and down-conversion, but small impact on total photocurrent**

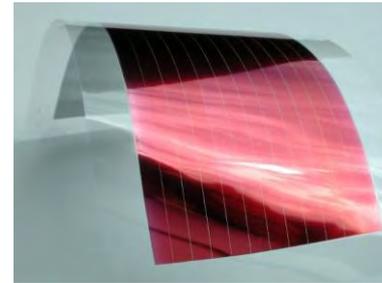
# Outline

- Photovoltaic energy conversion
- Limiting efficiency of solar cells
- Where next?
- Routes to more work per photon
- **Molecular solar cells**

# Thin films and emerging technologies



Amorphous Si  
 $\text{CuInGaSe}_2$   
 CdTe



Polymer:fullerene  
 Molecule:fullerene  
 Polymer:nanocrystal

Material	$E_g$ (eV)	Grain size ( $\mu\text{m}$ )	Max $J_{sc}$ ( $\text{mAcm}^{-2}$ )	Actual $J_{sc}$ ( $\text{mAcm}^{-2}$ )	$V_{oc}$ (V)	Efficiency (%)
Crystalline silicon	1.1	$>10^4$	43	42.7	0.706	25.0
Crystalline GaAs	1.4	$>10^4$	32	29.7	1.122	28.8
Polycrystalline Silicon	1.1	10-100	42	38.0	0.664	20.4
$\text{CuInGaSe}_2$	$> 1.0$	1	$< 45$	34.8	0.713	19.6
Cd Te	1.4	1	42	26.1	0.845	16.7
Amorphous Si	$\sim 1.7$	$<10^{-2}$	$\sim 23$	16.7	0.886	10.1
Organic	$\sim 1.6$	$<10^{-2}$	$\sim 24$	16.7	0.899	10.0

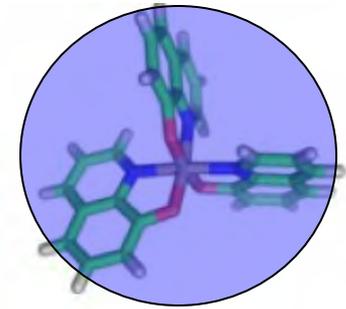
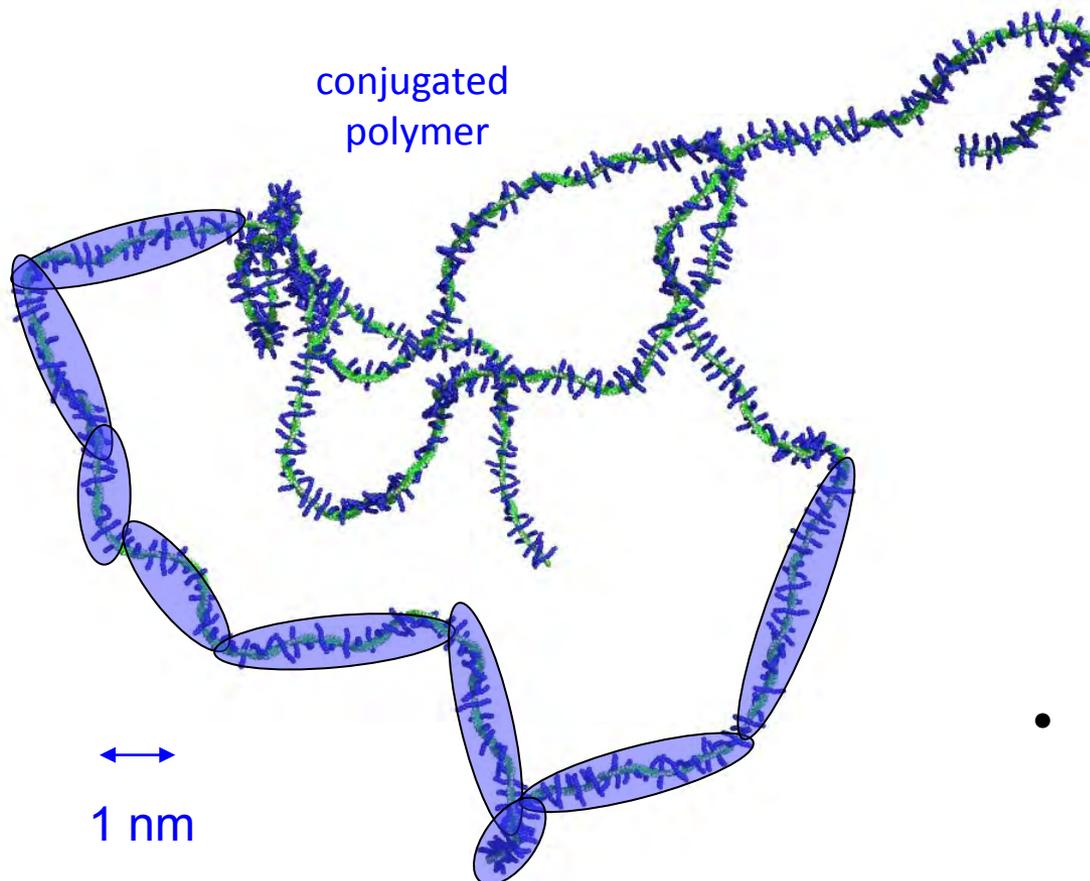
Single junction:  
 Limiting  $\eta$  as above

Practical  $\eta$  limited  
 by recombination:  
 small grains

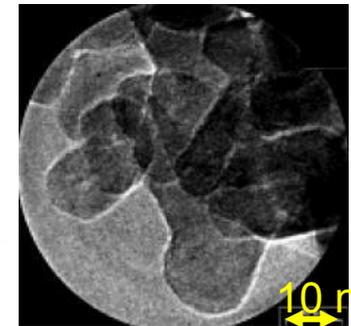
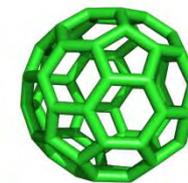
Heterojunction:  
 What limits  $\eta$  ?

# Molecular photovoltaic materials

- Excited states are localised:
  - Photogenerated charge pairs don't separate
  - Separated charges move slowly



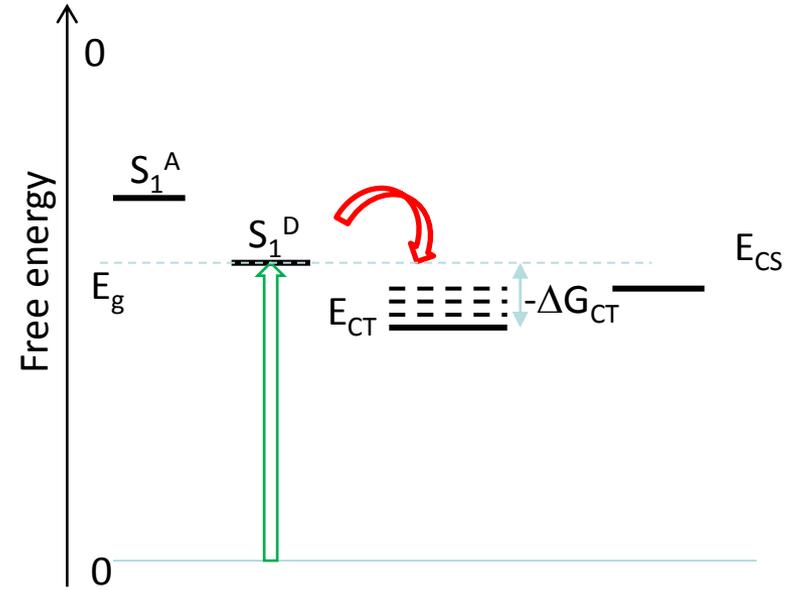
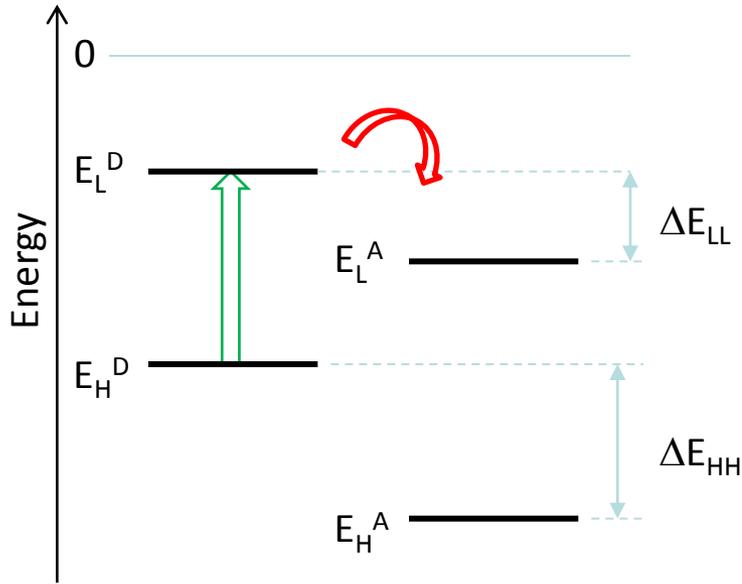
conjugated molecule



nanocrystal

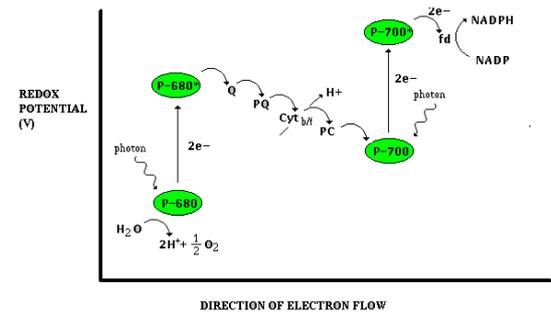
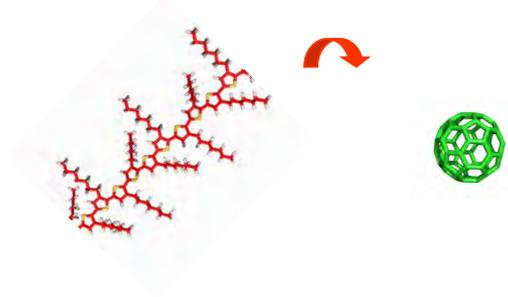
- Charge separation induced by doping with electron acceptors

# Molecular photovoltaic conversion

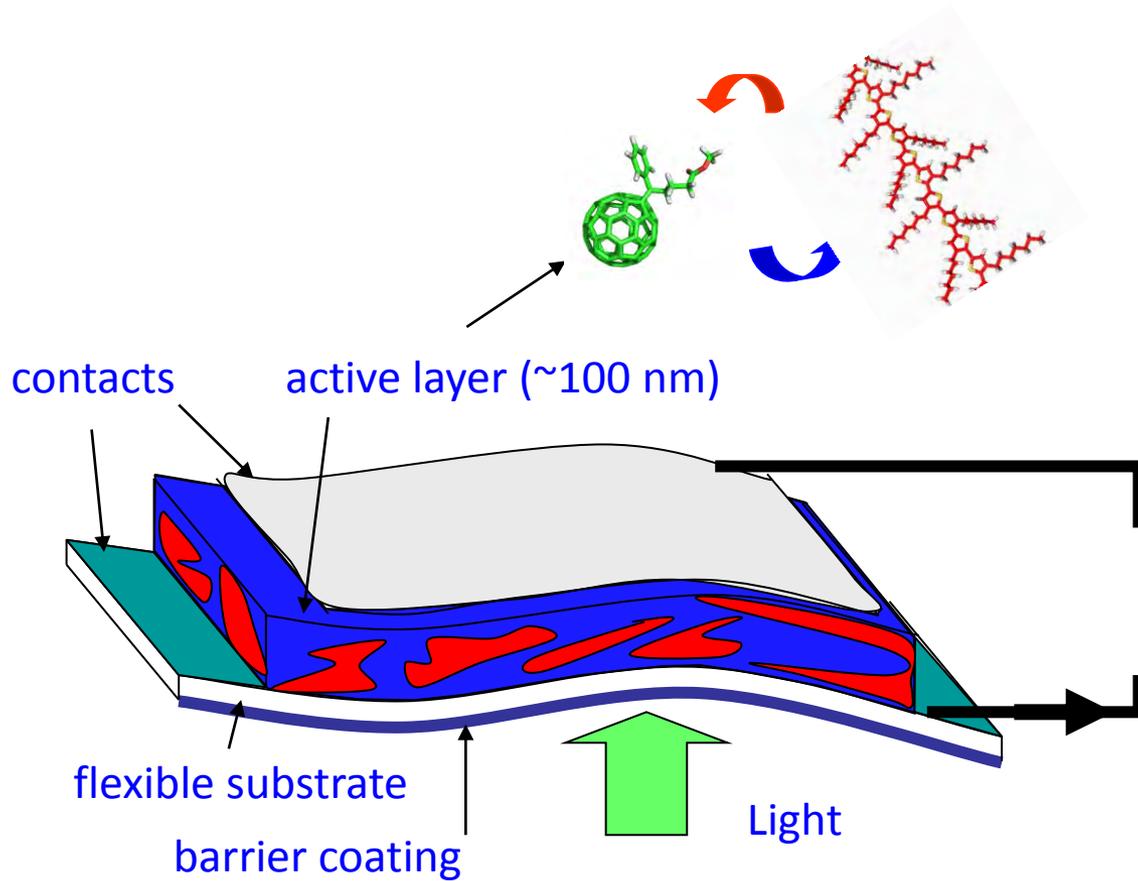


donor

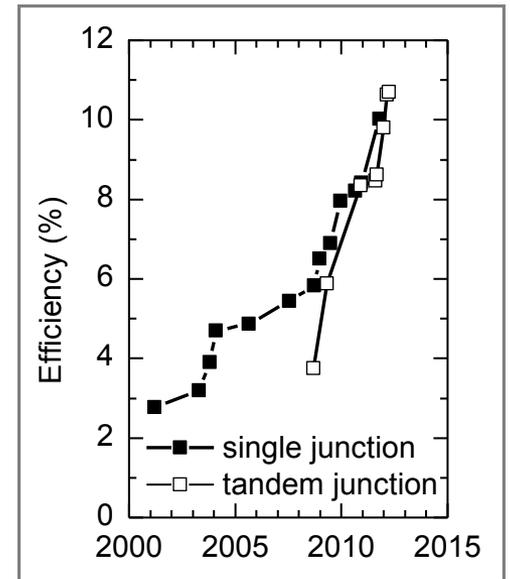
acceptor



# State of the Art in Molecular Photovoltaics

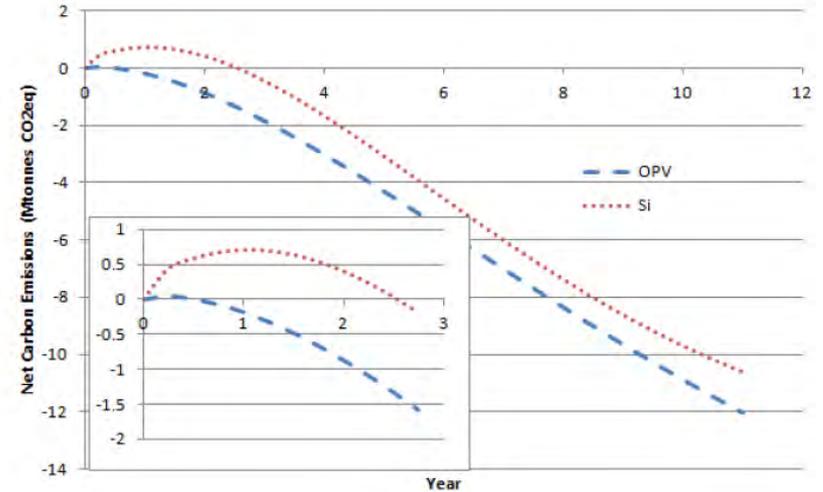
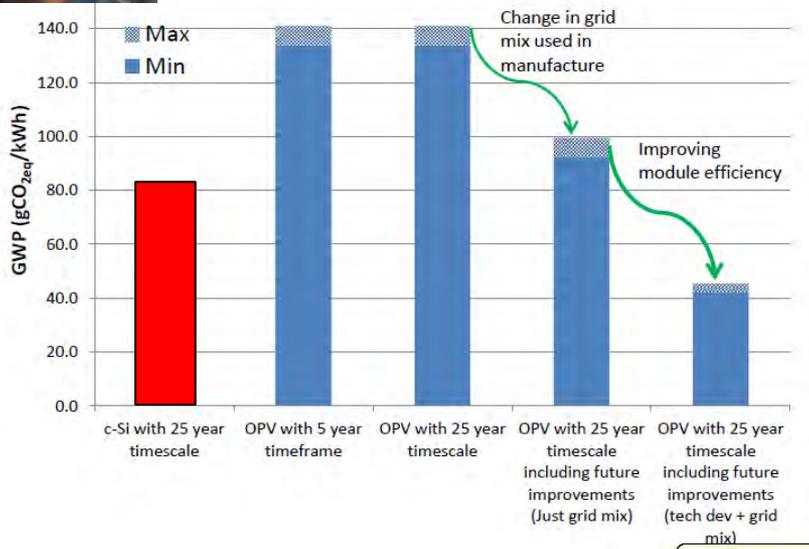
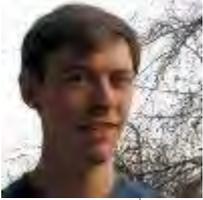


- Successive layers deposited from solution



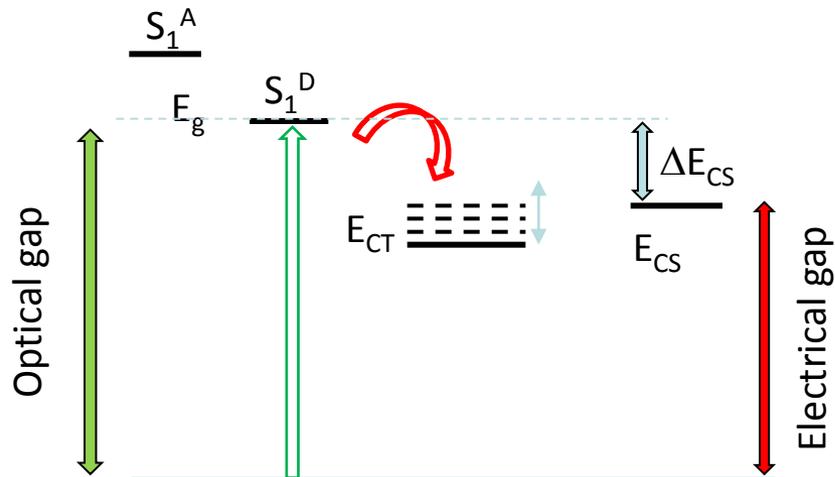
- Cell efficiency > 10%
- Modules follow slowly..

# Molecular Photovoltaics: Energy efficiency

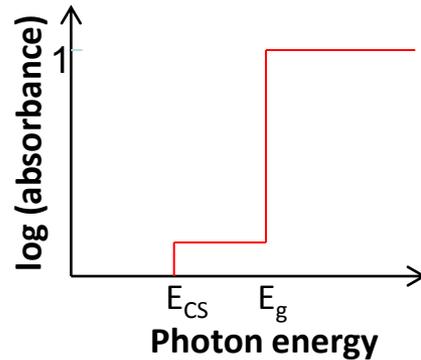


- Motivation is lower manufacture cost, but also lower energy intensity
- Enable larger impact on CO<sub>2</sub> emissions in short term, especially if lower cost stimulates faster uptake
- In long term, higher power conversion efficiency is key

# Limiting efficiency in molecular heterojunction

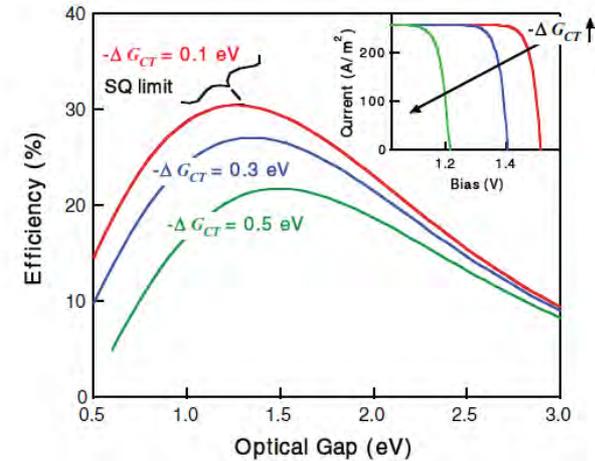
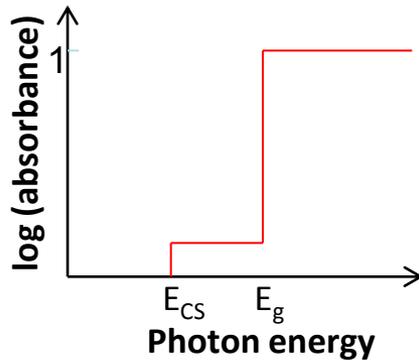


- Optical gap > electrical gap
- In detailed balance limit, charges recombine radiatively across electrical gap

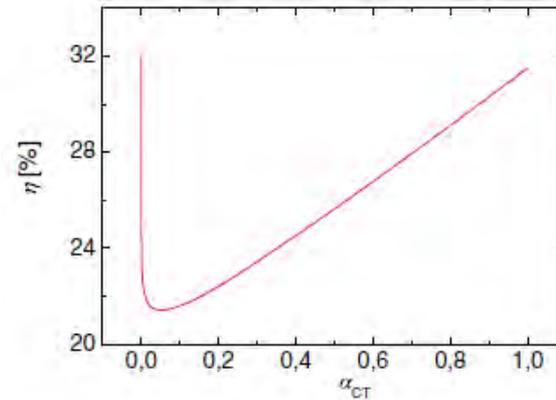


- Introduce sub-gap states of finite oscillator strength

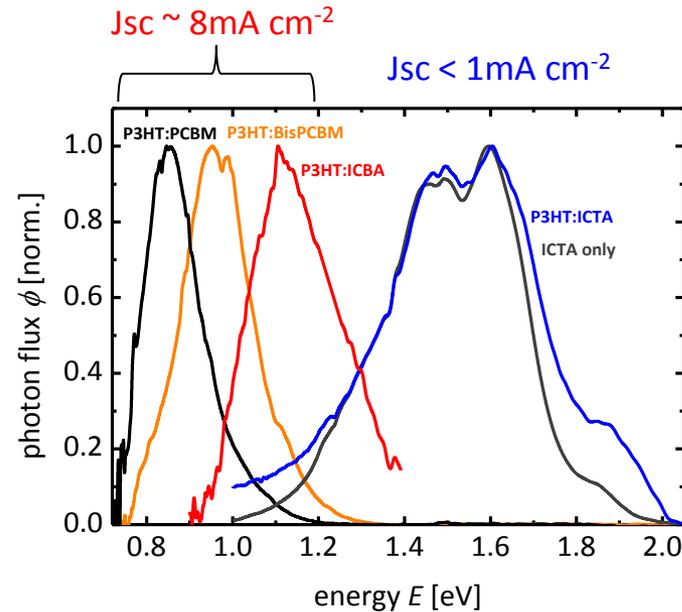
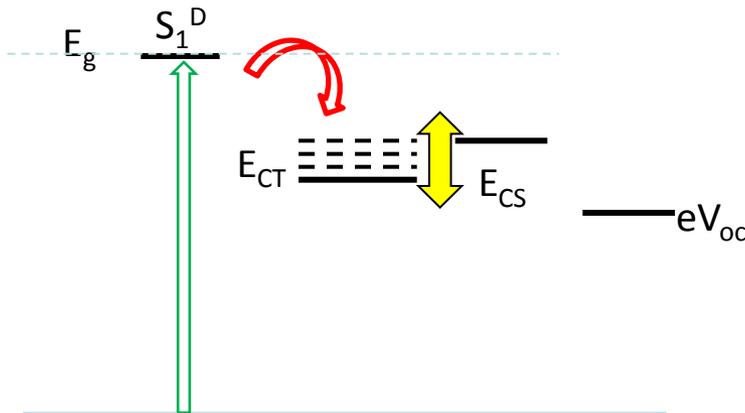
# Limiting efficiency in molecular heterojunction



- Limiting  $\eta$  is lower and optimum  $E_g$  larger than for single junction
- Most models predict 20%, practical best is 10%
- **Where are losses?**
- How large must  $(E_g - E_{CS})$  be?



# Size of energetic losses in molecular heterojunction

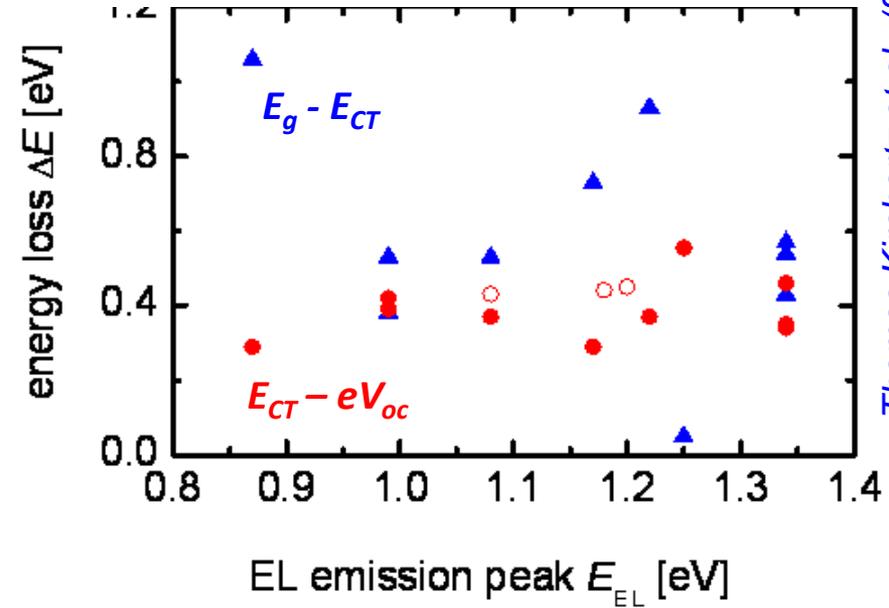
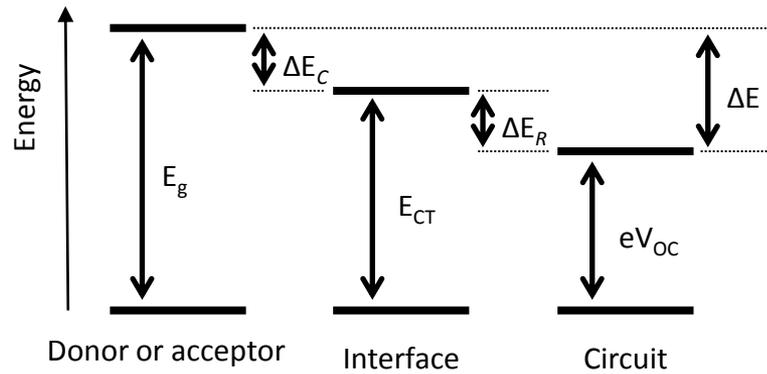


- Probe energy of charge pair at interface,  $E_{CT}$  with electroluminescence
- Modulate  $E_{CT}$  for same  $E_g$  by varying fullerene acceptor
- Find
  - photocurrent is generated only when  $(E_g - E_{CT}) > 0.35$  eV (with exceptions)
  - $eV_{oc}$  is smaller than  $E_{CT}$  (and  $E_{CS}$ ) by  $\sim 0.4$  eV

# Size of energetic losses in molecular heterojunction



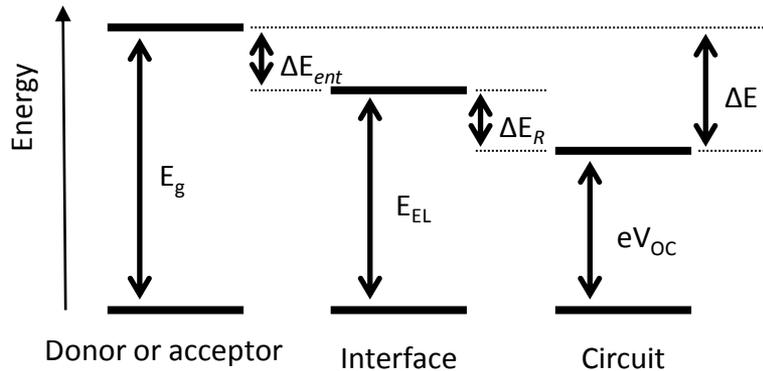
- Resolve energy loss  $\Delta E = E_g - eV_{oc}$  into two components:



Thomas Kirchartz et al., (2012)

- Charge separation loss**  $\Delta E_C$  normally  $> 0.3$  eV. Absent in inorganics.
- Non-geminate **recombination loss**  $\Delta E_R \sim 0.4$  eV, similar to inorganics
- Net  $E_g - eV_{oc} > 0.6$  eV, c.f 0.4 eV for inorganic single junctions

# Size of energetic losses in molecular heterojunction

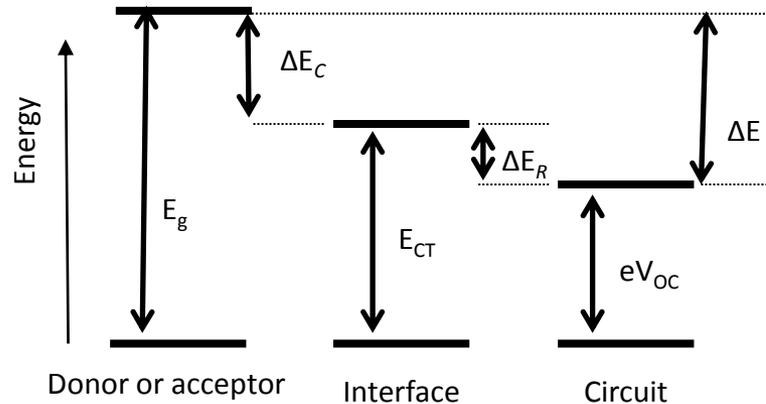


- **Inorganic junctions:**

$E_g - eV_{oc} \sim 0.4$  eV in best cases.  
Efficiency within  $\sim 5\%$  of DB limit

- **Molecular heterojunctions**

$E_g - eV_{oc} > 0.6$  eV



- Can we reduce  $\Delta E_C$ ?

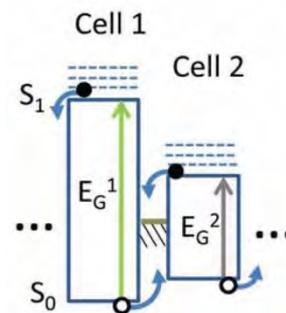
- Yes – in some cases,  $\Delta E_C$  as low as 0.1 eV

- Function of chemical structure
- But compensated by high  $\Delta E_R$
- Need to understand why!

# Molecular higher efficiency approaches?

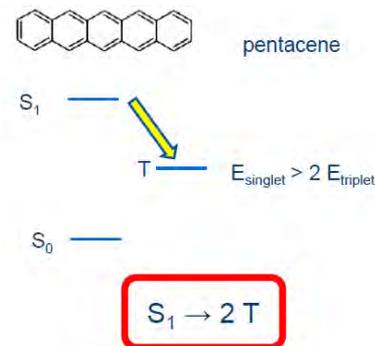
- **Multi junctions:**

- Tandems demonstrated.
- Easy to manufacture



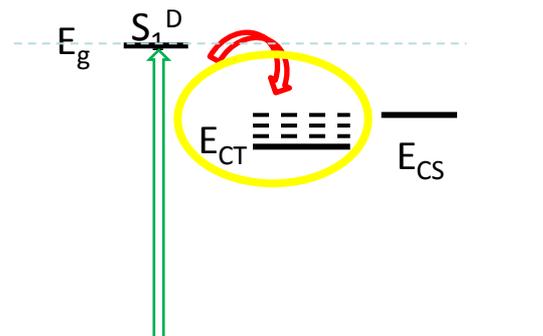
- **Spectral conversion:**

- Singlet exciton fission for downconversion
- Triplet-triplet annihilation for upconversion



- **Slow carrier thermalisation?**

- Helps to reduce losses to trapping at interfaces and in transport
- *Might* give access to hot carrier effects if energy selective contacts possible



# Where do we go from here?



- Solar electricity is abundant, sustainable, versatile and available
- Existing technologies operate within a factor of 2 of the physical limit of 30%
- Goal is to reach similar or higher efficiencies with low energy technologies that can grow quickly.
- Challenges remain for physicists, chemists and materials scientists – but none of them known to be insurmountable

**Thank you for your attention!**